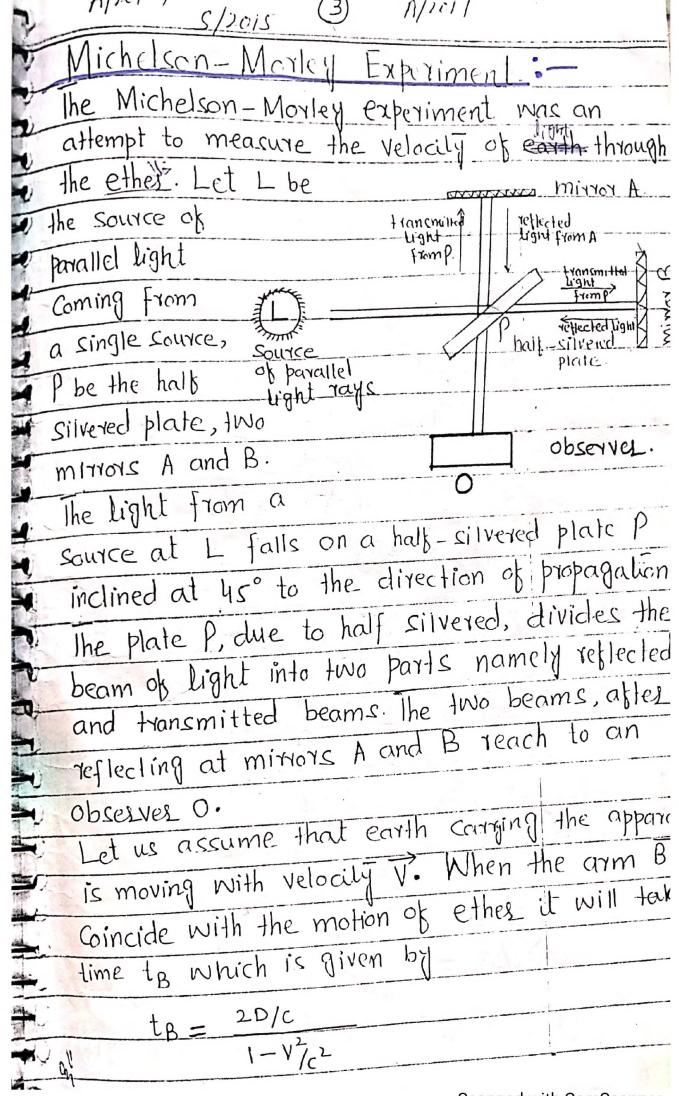
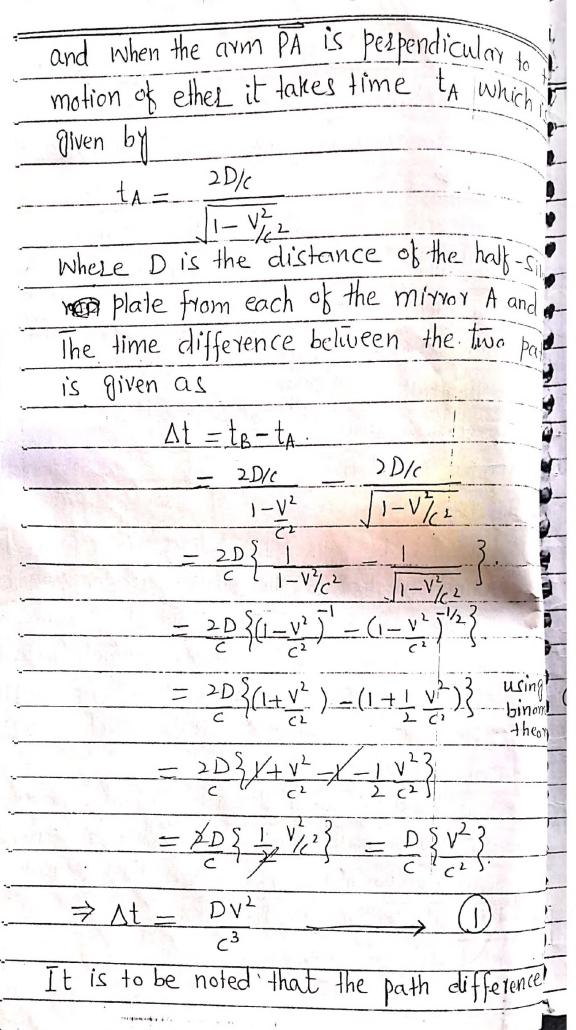
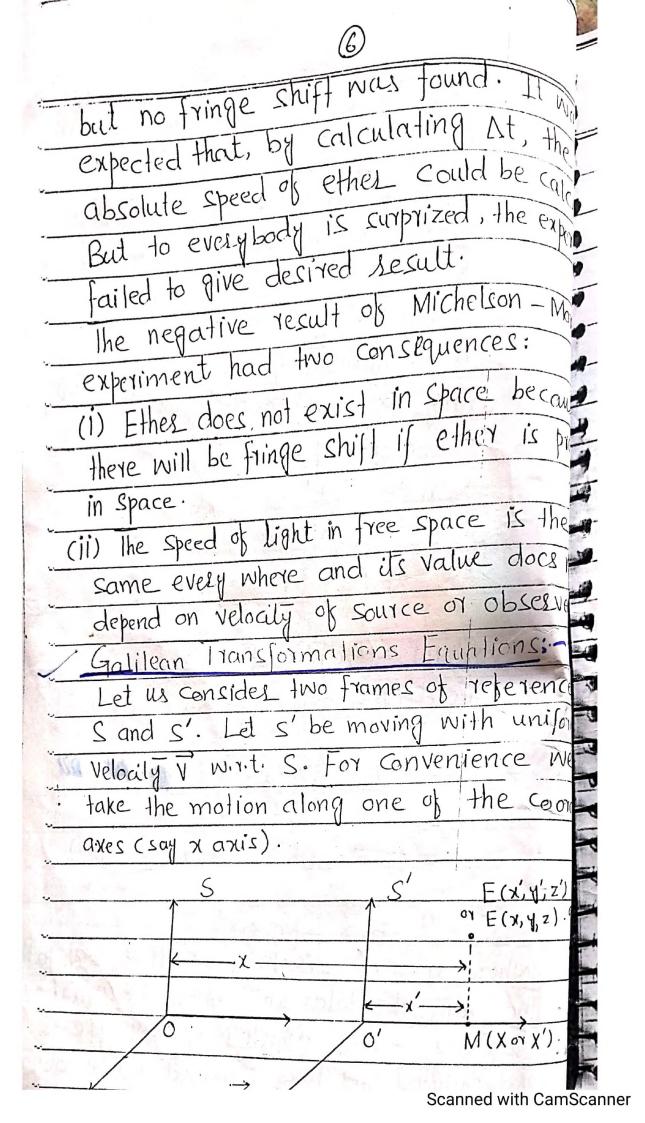
Quantum Mechanics The motion of objects sufficiently is studied in Quantum mechanics that discuss the atomic nature of matter with velocities Comparable with the velocities of light. Kelativistic Mechanics Relativistic mechanics concerned with the motion of bodies whose relative velocities approach the speed of light a Relative Velocity Let A and B be two objects moving uniform velocities Vi and Vi. Then related Velocity of object A wirt Bis Vi-Kelativistic Velocity Anyvelocity that is sufficiently high to signified changes in mass (or length or t of the object is called relativistic veloc Inalial Frame of refrience the frame of reference in which Newton's are valid is called inertial frame of reference Non-inertial frame of reference. The frame of reference in which Newton's are not valid is called non-inertial frame

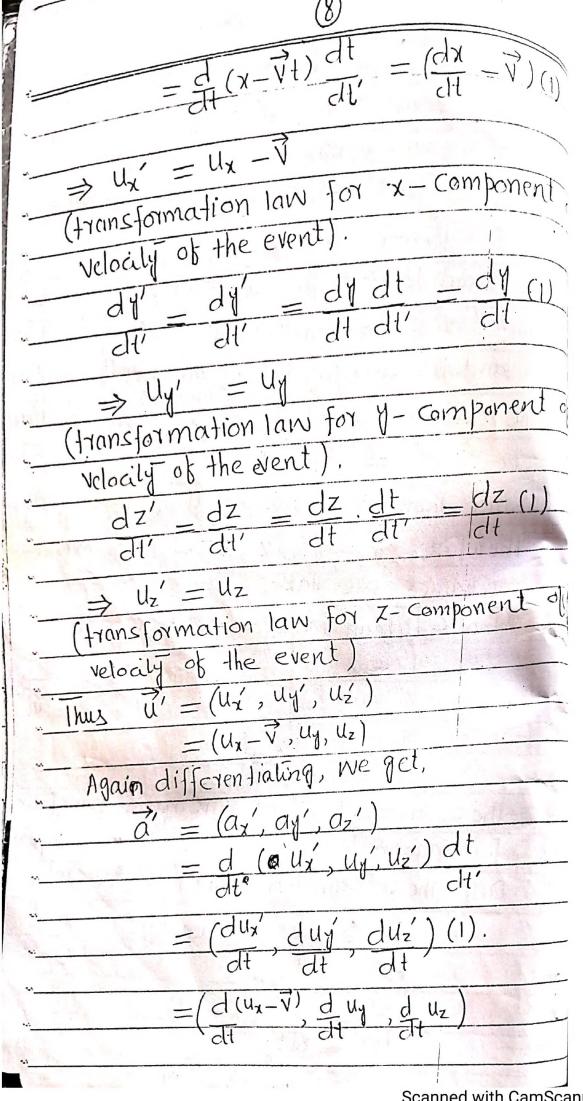


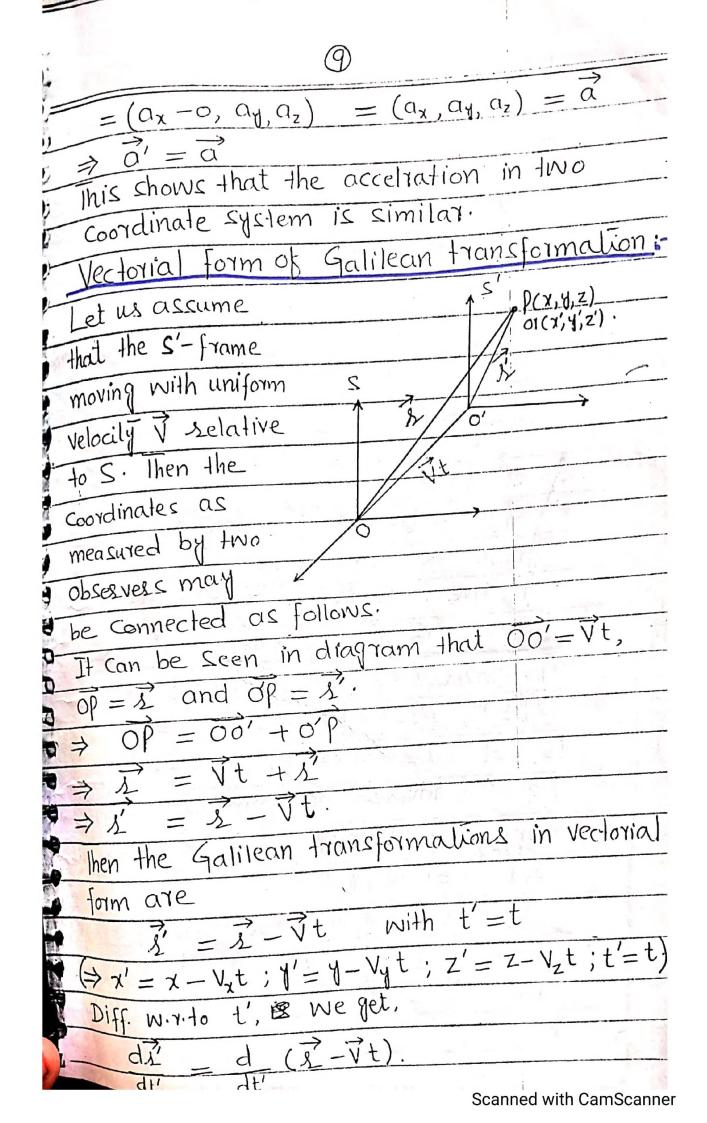


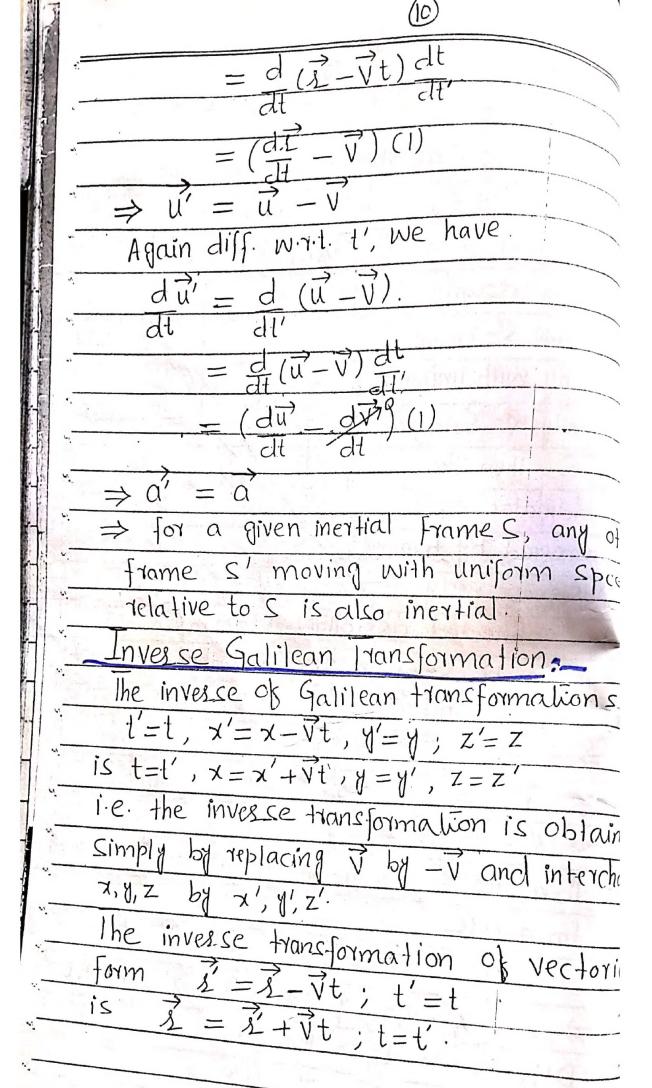
of two light waves related with this time difference is $d = c \Delta t$ and the path difference corresponding to shifting of fringes is $d = n\lambda$ where n is number of shifting of fringes. Comparing @ and 3, we get, $C\Delta t = n\lambda$ $\frac{n = C\Delta t}{\lambda} = \frac{C}{\lambda} \Delta t$ $=\left(\frac{C}{\lambda}\right) DV^{2}$ using O Morey used $D = 10 \, \text{m}$, $\lambda = 5 \, \text{x} \, \text{i} \, \text{o}^{7} \, \text{m}$ $\vec{V} = 3 \times 10^4 \,\mathrm{m/s}.$ n = $=(2\times10^{7})(10^{-4})^{2}=(2\times10^{7})$ 2 X10 0.2 Fringes. Where n = 0.2 is fringe shift of each path. Therefore, the total Shift must be equal to 2x0.2 = 0.4 which is of significant magnitude and was expected to be observed,



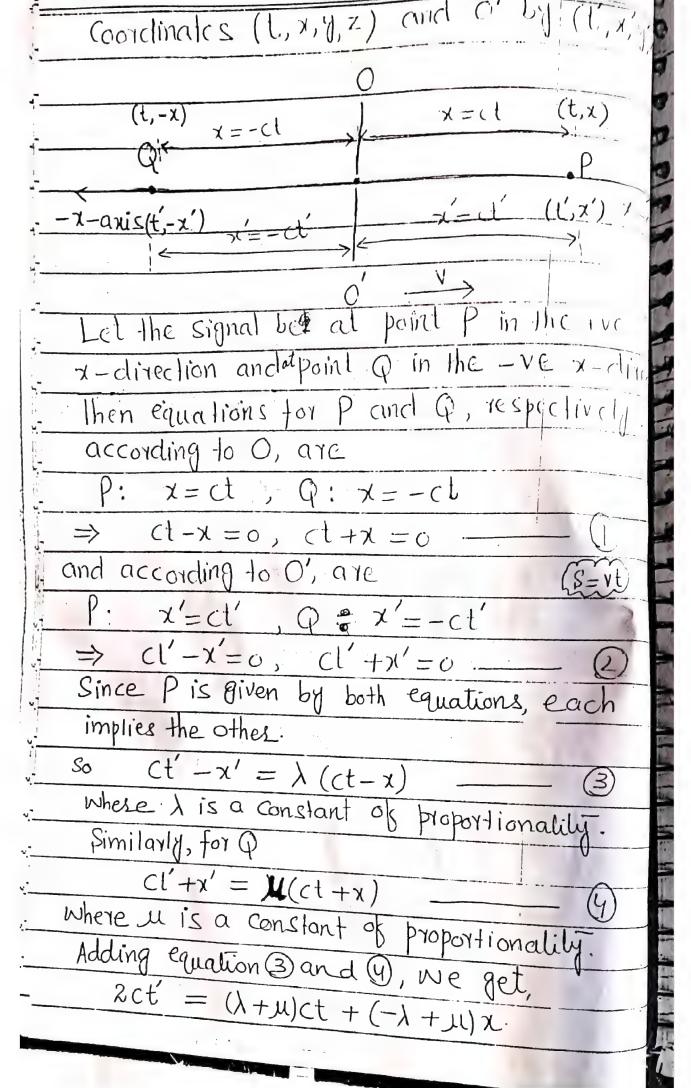
Further we assume that the coordinates
of an event are (x, y, z) at tas observed
of an event are (x,1,2) and say
The state of the Catalogical
(x', y', z') at t' as observed by an observer
6/ 5
The relation between constitution
and t, x, y, z. We note made and t, x, y, z. We note made and x' coordinates of the event, oo' is
and x' coordinates of me in time t
the distance converted by S-trame in time t
0.0/
is no motion along yor Z-ans,
Therefore, $y' = y$, $z' = z$ and in Newtonian
therefore, $V = V$, $Z - Z$
mechanics we take t'=t.
The Galilean transformations are
t' = t
$x' = x - \sqrt{t}$ $x = y + x'$
3 4' = 4
$\frac{0}{z'} = z$
these are classical Kinematic transformatic
for uniform linear motion with velocity V.
for uniform linear months.
Diss. these equations w.r.t. t', we get.
dt' = dt (idenlity).
dt' dt'
dx' = d(x-y).
$\frac{dx}{dt'} = \frac{d}{dt'}$

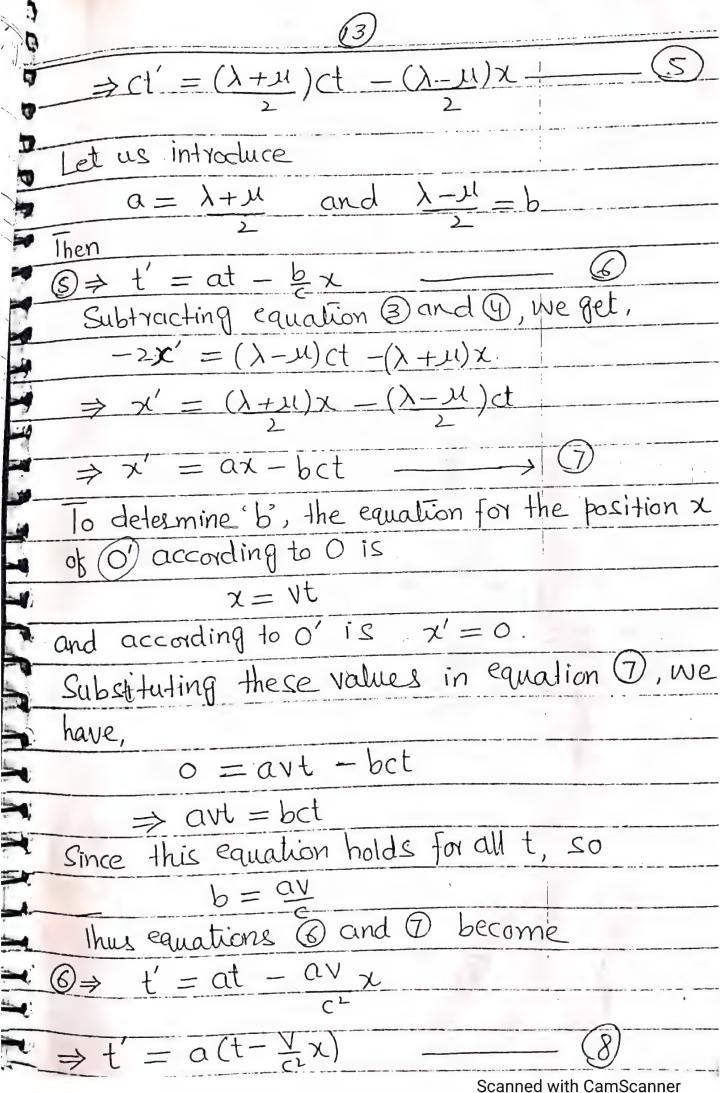


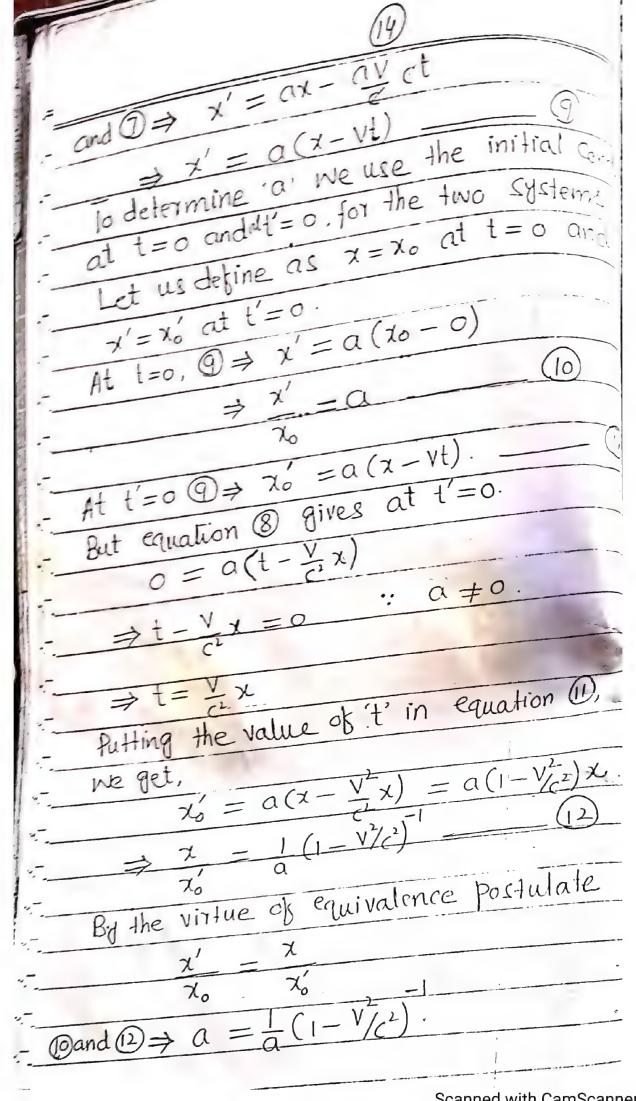




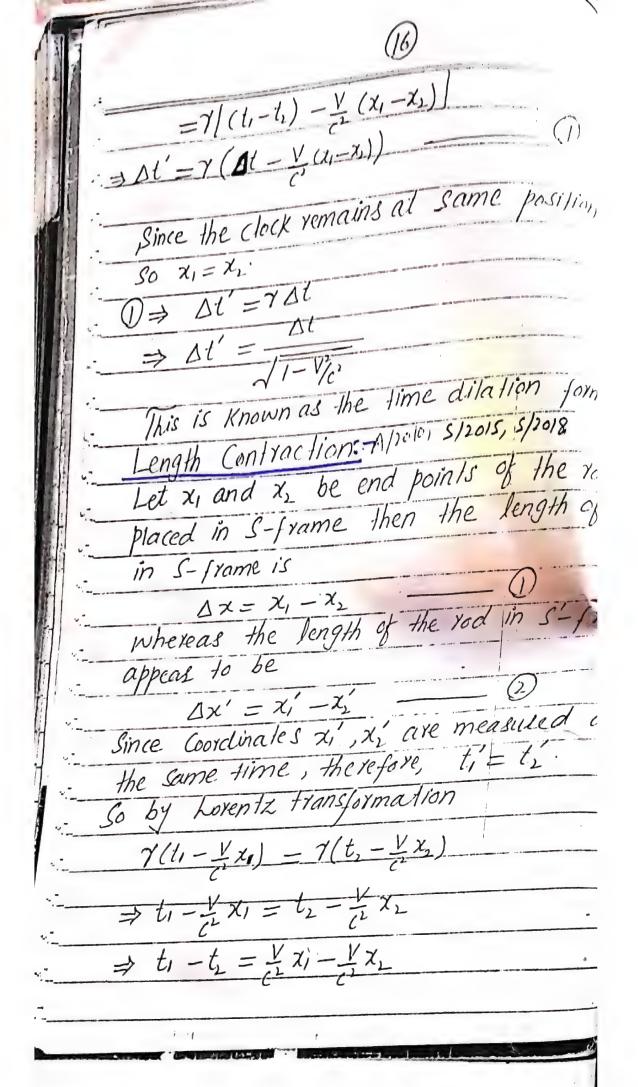
1
Postulates of Special Relativity:
il All the laws of physics are identical in
all inertial reference frames.
Till the Speed of light in fice space is constan
for all inertial reference frames. Its value
in free space is 3 ×108 m/s.
Postulate (i) is called the principle of relativity
and (ii) is called principle of constancy of
Grand of light.
Toxontz Izansformations: 1 5/2015, 5/2018
The cot of equations Which relates cocicinan
at a circle event in the different reference
frames are called Lorentz transformations.
Explanation.
Let us consider two observers 0 and 0
Such that the Observer O' is moving win
Speed V in the x-direction relative to U.
There two observes & coincide at one insta
and at that instant they start their clocks
They both send two light signals in the tv
and -ve x- exiditection.
Since the speed of light is the same for all
Since the speed of light is the same for all observers, therefore the signals travel
109ethes.
Let 0 measure time and space by the







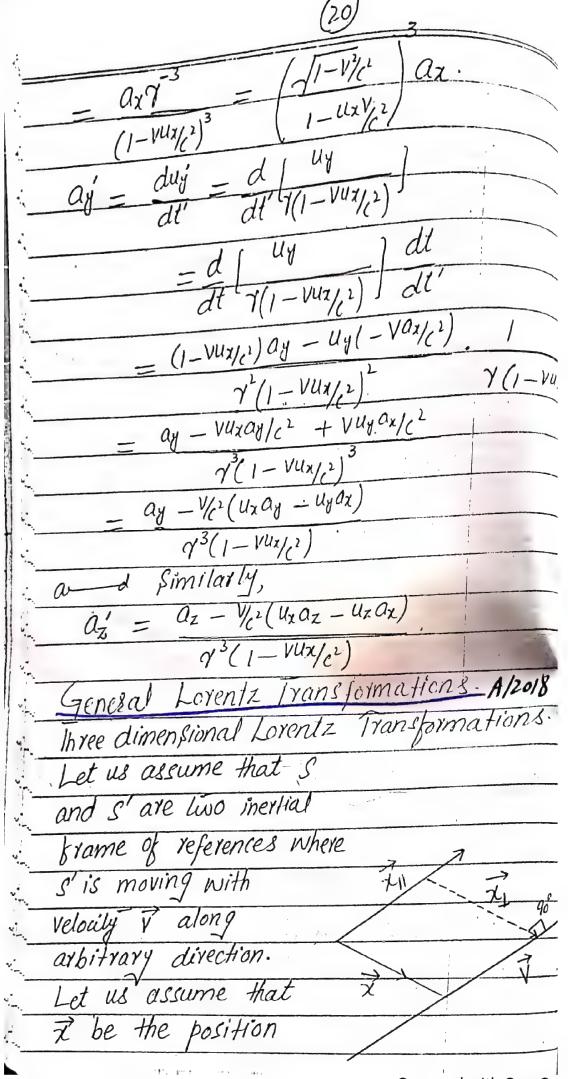
 $= \langle \alpha' = (1 \quad \forall \gamma \alpha')^{-1}$ => (1 = V/C) = 1/2 .) (l : 1-V'/62 The Losentz Transformations are $\otimes x = \alpha(1 - \frac{1}{2}x) = \frac{1 - \frac{1}{2}x}{2} = \gamma(1 - \frac{1}{2}x).$ $\mathfrak{D}(x') = \alpha(x - vt) = x - vt$ y (x. vl). y'= y and z'=z. Thus Lorentz transformations are purely kinematic and have no need to appeal to dynamics of electrodynamics. lime dilation: -1/2010, 5/2015, 5/2018, Let us consides two events in S frame occurring at time t, and t, then the time interval between the events is $\Delta t' = t_1 - t_2$. Let us assume that an observer in the frames Observes the same event at times to, and to we denote this time interval by DI = t_1-t_2. Then by Lorentz transformation $t'_{i} = \gamma(t_{i} - \frac{\vee}{2}x_{i}), t'_{i} = \gamma(t_{i} - \frac{\vee}{2}x_{i})$ where $\gamma = \frac{1}{1-v^2}$ Thus $\Delta t' = \gamma(t_1 - \frac{V}{2}x_1) - \gamma(t_2 - \frac{V}{2}x_2)$.

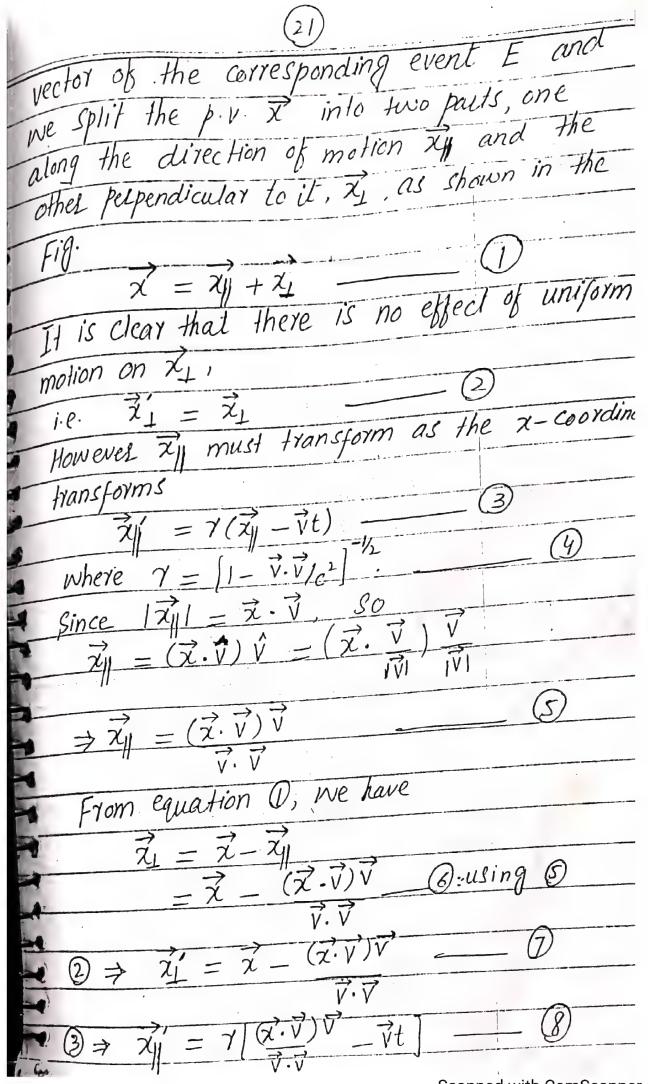


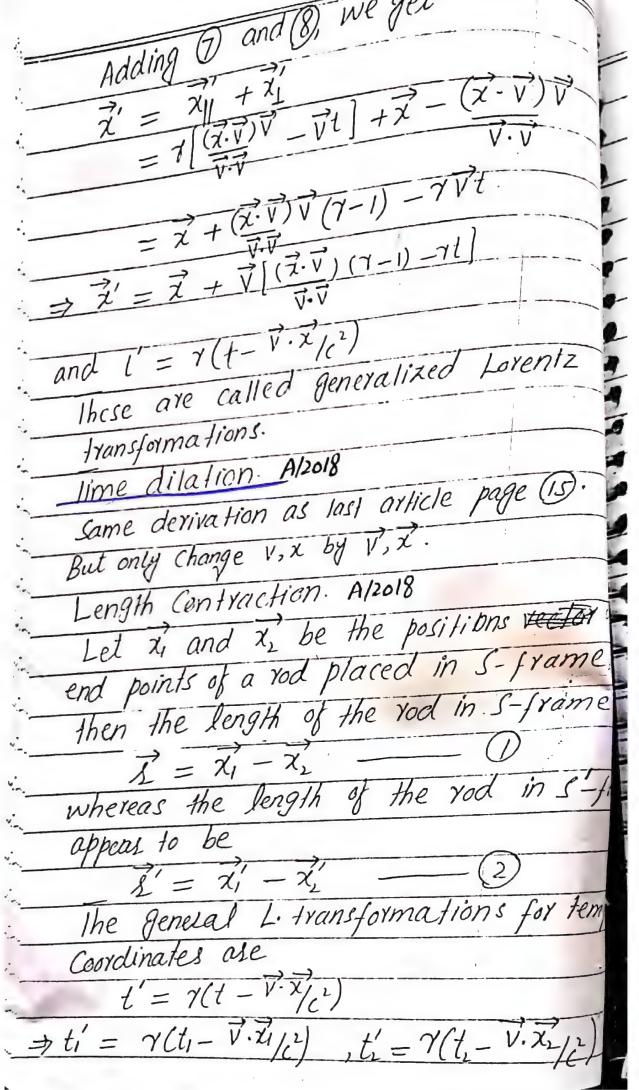
₹,
\sim (7)
$t_1 - t_2 = \frac{V(\chi_1 - \chi_2)}{2}$
$\frac{1}{2} \frac{t_1 - t_2}{t_1 - t_2} = \frac{V}{V} \Delta x \qquad \qquad \boxed{3} using (1)$
Again using the Lorentz Transformations
$\chi_1 = \gamma(\chi_1 - 1/4)$
$\chi_{i} = \gamma(\chi_{i} - vt_{i}), \chi_{i}' = \gamma(\chi_{i} - vt_{i})$ $Q \Rightarrow \Lambda \chi' - \gamma(\chi_{i} + vt_{i})$
$2 \Rightarrow \Delta x' = \gamma(x_1 - vt_1) - \gamma(x_1 - vt_2)$
$= \gamma[(\chi_1 - \chi_2) - v(t_1 - t_2)] = \emptyset$ Substituting earlier (2):
substitution (3) in (4), we get
$\Delta x = \gamma [\Delta x - V^2 \Delta x]$
$-\gamma(1-\sqrt{1-2})$
$= \gamma(1 - V_{(c)}) \Delta x = \gamma \gamma^{-2} \Delta x$
$=\Delta x$
7.
$\Rightarrow \Delta x = \Delta x / 1 - v / 2 \qquad : \gamma = \sqrt{1 - v / 2}$
$ A \Rightarrow \Delta x = \Delta x / 1 - v^2/2 \qquad : \gamma = \frac{1}{1 - v^2/2}$ This is called the Lorentz-length Contraction. Relativity of Cimulton with
Mauring of primatarely
Consider two events that appear simultaneous
to an observer 0 in S-frame, i.e. one occurs
at x, and the other at x, at the same
lime, or in other words $t_1 = t_2$.
The two events would be simultaneous
according to 0' if t' = t' but this is not
Possible infact $t_1' - t_2 = \gamma / (t_1 - t_2) - V (x_1 - x_1)$
$t_1'-t_2'=\gamma[(t_1-t_2)-\frac{V}{C^2}(\chi_1-\chi_2)]$
(L

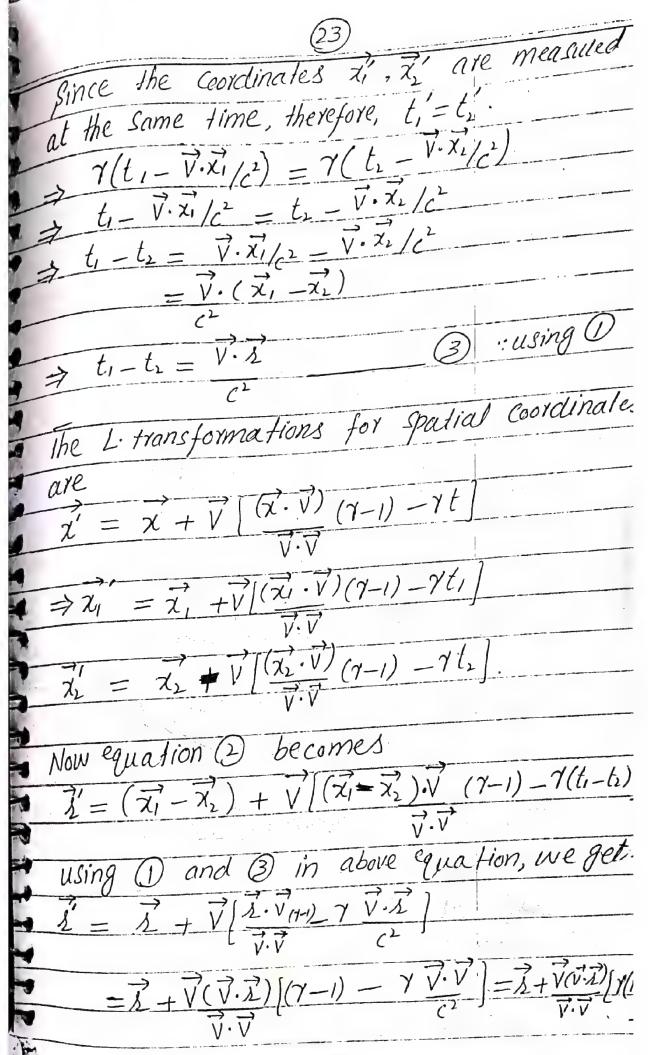
(18)
V / v VI)
$= 7(0 + \frac{1}{2}(x, -x_1))$
$\Rightarrow t_1 - t_2 = \frac{7}{2}(x_1 - x_1) \neq 0$
: => 1-6-1/
titt.
$\frac{1}{1}$
according to 0'. Hence simultaneity is
rolative.
Velocity Addition formulae.
By Lorentz transformation
$t' = \gamma(t - \frac{1}{2}, x)$
$x' = \gamma(x - vt) ; y' = y ; z' = z$
$\Rightarrow dt' = \gamma(dt - \frac{V}{C^2}dx)$
$dx' = \gamma(dx - Vdt) ; dy' = dy; dz' = dz$
By definition of the Speed of any object
the x, y and z directions according to
$u_{x} = dx u_{y} = dy u_{z} = dz$
Ole all
: Thus dx' = 7(dx-vdt) = dx-vdt
dl' 7(dt-1/2dx) dt-1/2dx
$\frac{1-y}{2}\frac{dx}{dt} = \frac{1-vux}{1-vux}$
$dy' = dy = \frac{dy}{dt}$
$\frac{dt'}{2} \gamma \left(\frac{dt - \frac{v}{2} dx}{2t} \right) \qquad \gamma \left(1 - \frac{v}{2} \frac{dx}{dt} \right)$
$= \qquad \qquad$
$\frac{d(1-V^{4x}/c^{2})}{\text{Scanned with CamScan}}$

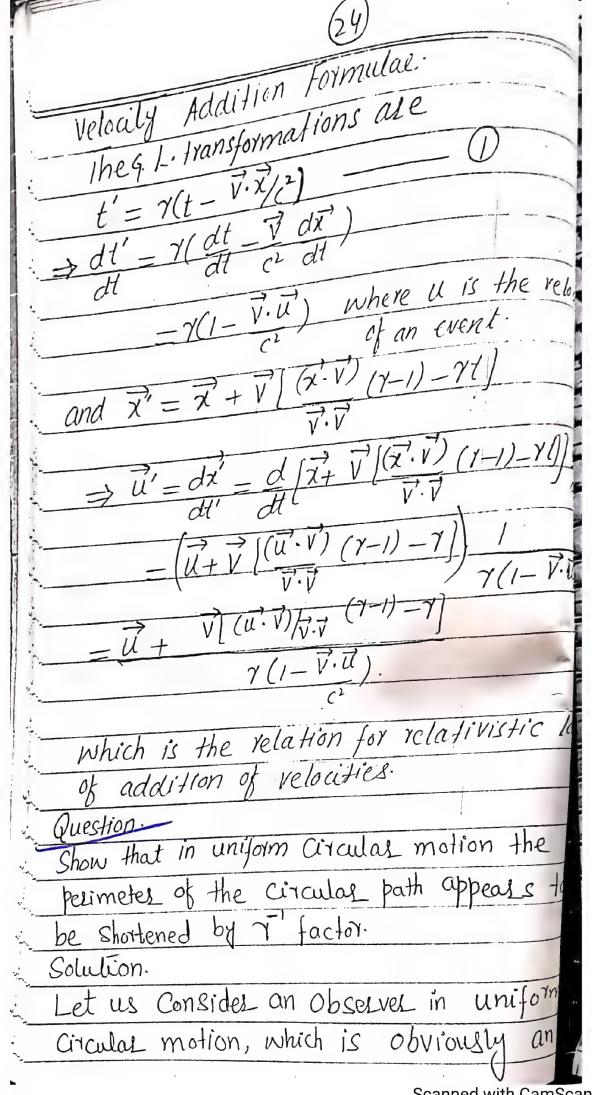
$\int dz' = dz \qquad dz/dt$
and $\frac{dz'}{dl'} = \frac{dz}{\gamma(dl - v dx)} = \frac{\frac{\partial^2}{\partial t}}{\gamma(l - v \frac{\partial^2}{\partial t})}$
2 1/2 = Uz
$\gamma/1 - V(\chi/1)$
These are the required velocity addition
1
Distinicic Components of Acceptation
We can find the relativistic Components of
accelration by defining
$a_x = \frac{du_x}{dt}$, $a_y = \frac{du_y}{dt}$, $a_z = \frac{du_z}{dt}$.
$\frac{dt}{du_{2}'} = \frac{du_{2}'}{du_{2}'} = \frac{du_{2}'}{du_{2}'}$
and ax - dt', d' - dt'
where $a_{x'} = d \left[\frac{u_{x} - v}{v_{x'}} \right] = d \left[\frac{u_{x} - v}{dt} \right] dt'$
$\frac{d^{2}-\sqrt{2}}{c^{2}}$
where di' = r(dt - vdk)
a $VU_{X}(x)$
$= \gamma(1 - \frac{vu_{\chi/2}}{c^2})$ $= \gamma(1 - \frac{vu_{\chi/2}}{c^2}) (a_{\chi} - 0) - (u_{\chi} - v) (-\frac{vo_{\chi/2}}{c^2}) \cdot \gamma(1 - \frac{vu_{\chi/2}}{c^2}) \cdot \gamma(1 - \frac{vu_{\chi/2}}{$
$\frac{\left(1-\frac{Vu_{x}}{C}\right)^{2}}{C^{2}}$
$- \alpha_{\chi}(1-VU_{\chi/c^2}) + \frac{1}{2}(U_{\chi}-V)\alpha_{\chi}$
$\frac{\gamma(1-vux/2)^{3}}{2vux/2}$
$= 0x - VU\chi Q\chi /c^2 + \chi VU / C = 1$
$\gamma(1-Vu_{2}/c^{2})^{3}$
$= a_{x} \left(1 - \frac{V^{2}/c^{2}}{2}\right) - a_{x} q^{-1}$
7(1-V4x/c2)3 7(1-V4x/c2)3







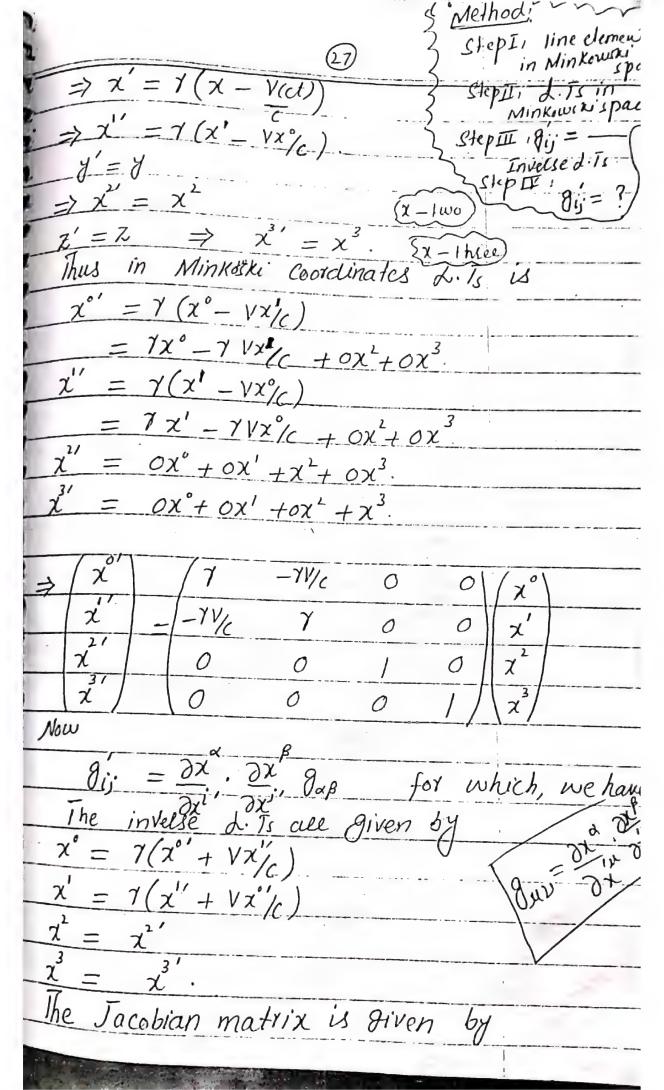




You ler directio accelerated motion. We assume that the meter rods Constitutes its diameter and the Circumference. Let us further assume that P = perimeter of the circle observed by an Observer O and d = diameter of the circle observed by an observer O. The ratio of the belimetel to its diameter is P/d. Let P' and d' be the perimeter and the diameter as observed by the observer O'. the rode making up the circle itself, can be assumed in the same direction as that of the instantaneous motion of O. Thus the lengths of the rod making up the circle are shortened by T' factor. Thus P'= Perimeter observed by O' is shorten by the factor T. the motion of O' wir. t. the rods making up the diameter is such that V is such I to diameter d, i.e. V. d'= o. ⇒d'=d (i.e. unaffected length of diameter) > The ratio of perimeter p' and d' = P/d' 7 p = 1 (p) = 1 x =

AUGI OF

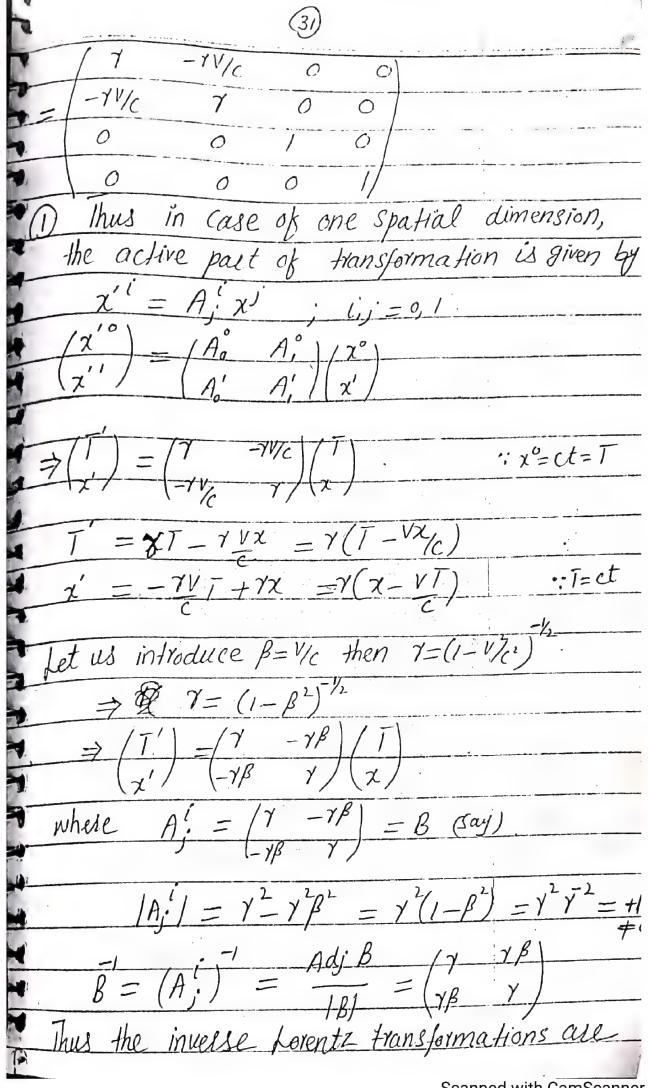
L'I' = TIT = CARE IS non- E
Thus p'd' = 7 x # This case is non-Euc i.e. the geometry in this case is non-Euc
i.e. the geometry
Positive de finite metric. A metric ds= 8ij dx'dx' is said to i
1 matric (1) - UI
positive definite if ds > 0.
positive argument
Indefinite metric.
Indefinite metric. A metric $ds^2 = \theta_{ij} dx^i dx^j$ is said to b
indefinite it ds'20.
Qualian C/2018
Show that line element is invalient
Show that the dands
Lorentz transformations.
Solution.
The line element in Minkoski Coordinas
is given by
$ds^2 = g_{ij} dx^i dx^j$
$= c^2 dt^2 - dx^2 - dy^2 - dz^2$
$\Rightarrow \theta_{00} = 1; \theta_{11} = -1; \theta_{12} = -1; \theta_{33} = -1$
(x, x, y, z) = ((1, 2, y, z))
$g_{ii} = 0 \forall i \neq i$
The L. Is in Minkowski:
The L. Is in Minkoski Coordinate ase
$\frac{t'=\gamma(t-Vx/2)}{(t-Vx/2)}$
$\Rightarrow (t' - x/(t -$
$\Rightarrow ct' = \gamma(ct - vx/c)$
$= \gamma (\gamma^{\circ})$
$\chi' = \gamma(\chi - Vt)$

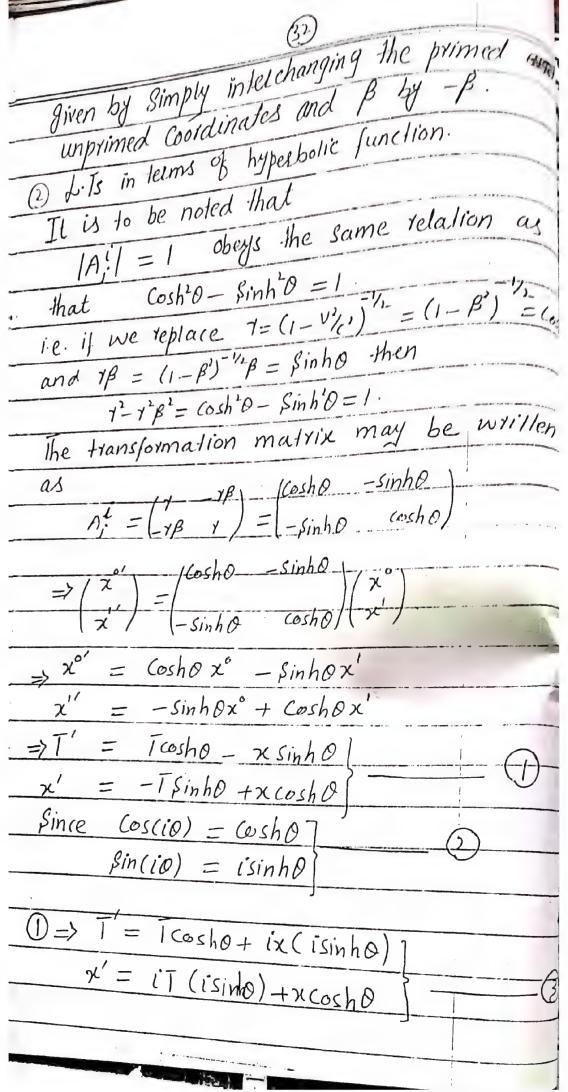


28
(3x/: 3x/2' 0x/2' 3x
12x" - 2x/22 2x/2x 3x/2x 3x
(3x') 3x/2 3x/2x' 3x/2x' 3x
3/1/2/2/2/
3x/2x 3x/2x 0x/3x 0x,
/7 m/c 0 0
$= \gamma V_{/C}, \gamma \rangle = \gamma V_{/C} $
0 0 1 0
Now & B
$g_{ij} = \frac{\partial x}{\partial x^i}, \frac{\partial x}{\partial x^j}, g_{\alpha\beta}$
$g'_{00} = \frac{\partial z^{\alpha}}{\partial z^{\alpha'}} \frac{\partial z^{\beta}}{\partial z^{\alpha'}} \frac{\partial z^{\beta}}{\partial z^{\alpha'}}$
$= \frac{\partial x^{\circ}}{\partial x^{\circ}} \frac{\partial x^{\circ}}{\partial x^{\circ}} \frac{\partial x^{\circ}}{\partial x^{\circ}} \frac{\partial x^{\prime}}{\partial x^{\circ}} \frac{\partial x^{\prime}}{\partial x^{\circ}} \frac{\partial x^{\prime}}{\partial x^{\circ}}$
$\frac{1}{1+\frac{\partial x^2}{\partial x^2}\frac{\partial x^2}{\partial x^2}\frac{\partial x^2}{\partial x^2}\frac{\partial x^2}{\partial x^2}\frac{\partial x^3}{\partial x^3}\frac{\partial x^3}{\partial x^3}}$
$= \frac{(\partial x^{\circ})}{\partial x^{"}} \frac{g_{00}}{\partial x_{0}} + \frac{(\partial x^{'})}{\partial x_{0}^{"}} \frac{g_{11}}{\partial x_{0}^{"}} + \frac{(\partial x^{'})}{\partial x_{0}^{"}} \frac{g_{22}}{\partial x_{0}^{"}} \frac{g_{22}}$
$=7^{2}(1)+(7\sqrt{6})^{2}(-1)+0+0$
$= \gamma^2 - \gamma^2 V_{C^2}$
$= \frac{\gamma^2(1 - \frac{V_{1/2}^2}{2})}{2} = \frac{\gamma^2(\gamma^{-2})}{2} = 1$
-7000 = 1

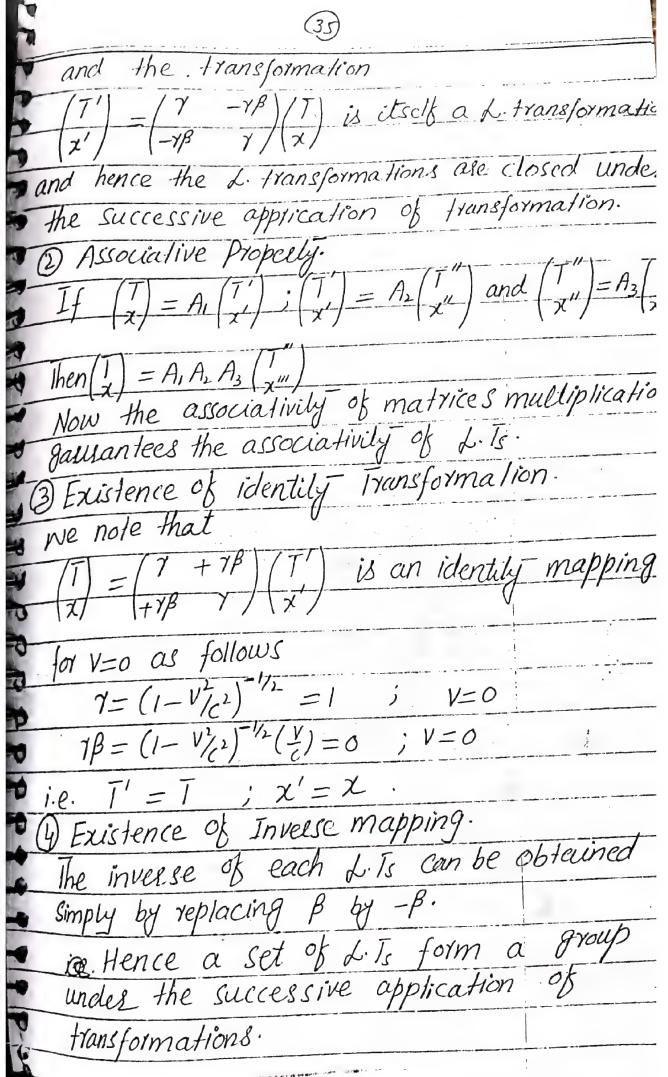
TI.	
M	(2q)
11	$\theta_{\parallel} = \partial x \partial x \theta \partial x$
10	$\frac{\partial x'}{\partial x} = \frac{\partial x'}{\partial x} \frac{\partial x'}{\partial x} \frac{\partial \alpha \beta}{\partial \alpha \beta}.$
	$= \sqrt{3} \times \sqrt{2}$
	$= (\frac{\partial x}{\partial x'}) g_{00} + (\frac{\partial x}{\partial x'}) g_{11} + (\frac{\partial x}{\partial x'}) g_{21} + (\frac{\partial x}{\partial x'}) g_{32}$
	$= (7\sqrt{2})(1) + (1)(1) + 0 + 0$
-	
-	= 72/22 -72
	$=-\gamma^{2}(1-\frac{1}{2})^{2}=-\gamma^{2}(\gamma^{2})=-1$
1	$\Rightarrow \theta_{n}' = -1$
1	8: - 1/2x° 10 ,0x' 19 ,12x' 19 ,12x' 10
1	$g_{11} = (\partial x^{\circ}) g_{00} + (\partial x') g_{11} + (\partial x') g_{11} + (\partial x') g_{3}$
-	
<u>.</u>	= 0 + 0 + (1)(4) + 0 = -1
	$\Rightarrow g_{12} = -1$
-	$g' = (\partial x)g_{00} + (\partial x')g_{11} + (\partial x)g_{22} + (\partial x)g_{33}$
1	DX' DX' DX'
13	= 0 + 0 + 0 + (1)(-1) = -1
5	$\Rightarrow 833 = -1$
	Therefore,
	$ds^2 = \theta_{ij} dx^i dx^j$
	$\frac{(1)}{(1-1)^{1}} \frac{(1)}{(1-1)^{1}} \frac{(1)}{(1-$
2	$= \theta_{ij} dx^{i'} dx$
-0-	$= \theta_{00} (dx')^{\frac{1}{2}} + \theta_{11} (dx'')^{\frac{1}{2}}$
4	$+ g_{11} (dx^{2'})^{2} + g_{33} (dx^{3'})^{2}$
-	- (1) (c2dt 2) - dx2-dy2-dz
	· = (2dt'2 - dx'2 + dy'2 - dz'2
0	$\Rightarrow ds^2 = ds'^2$
W	
1.13	Hence proved

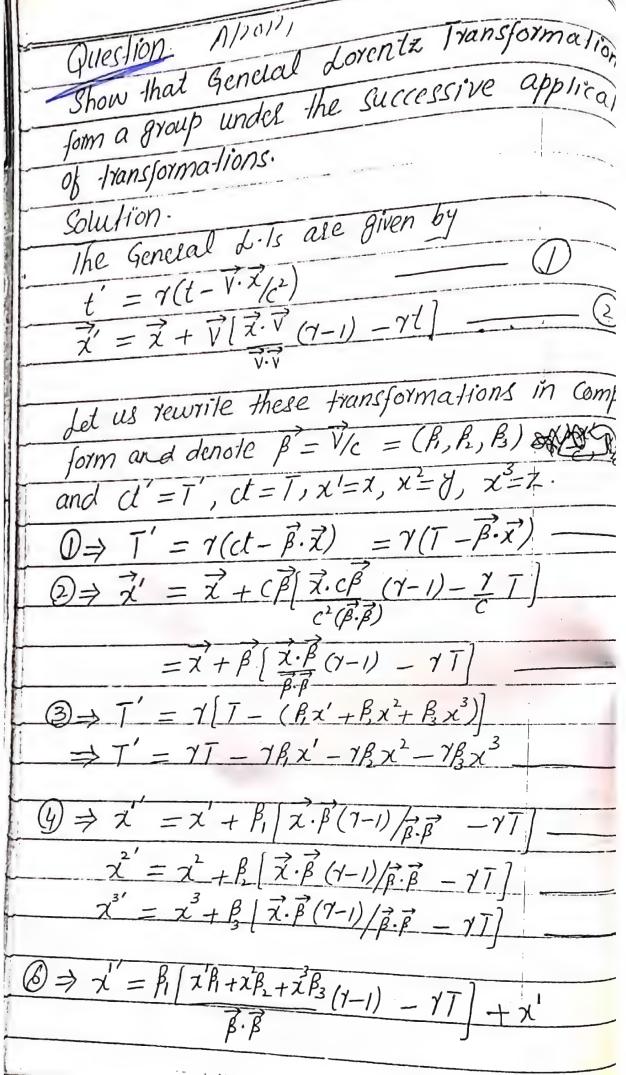
(30)
Tions in 4- vectors
The L. Transformations in q-matrix. The L. Transformations $(x, x', z) = (x', x', z)$
The L. Transfermate (ct, x, y, z) = (x, x, x)
The Coolain De vi 100
$\chi = \frac{1}{10000000000000000000000000000000000$
> z'0 = A. X A' x + A, X + A;
$\chi' = A_1 \times \frac{1}{2} = \frac{1}{2} \times 1$
$\chi'^{2} = A_{1}^{2}\chi^{3} = A_{0}^{3}\chi^{4} + A_{0}^{3}\chi^{2} + A_{0}^{3}\chi^{2}$
$\frac{1}{2^{3}} = A_{i} x^{j} = A_{o} x + H_{i} x + H_{i} x$
10 Az (x°)
1/2'0 /A. A. //2
1 A' A' A'
$\begin{vmatrix} \chi & = H_0 \\ \chi^2 & A^2 & A^2 \\ \chi^2 & A^2 & A^3 \end{vmatrix} \chi$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
To 1 To can be written as
The wist way)
$\frac{ct}{x''} = \gamma(x'' - vx') = \gamma x'' - \gamma vx' + ox' + ox'$
$\frac{1}{2'} = \frac{1}{2}(x - yt)$
$= \frac{\chi}{(\chi - Vct)} = \frac{\gamma(\chi' - V\chi'/c)}{\chi'}$
$= \frac{7(\chi - vc^2)}{c^2} = \frac{7V\chi^0 + 7\chi' + 0\chi^2 + 0\chi^2}{2}$
$\frac{1}{2} \frac{1}{C} \frac{1}$
$y' = y \Rightarrow \chi = \chi = 0\chi + 0\chi + \chi^{3}$ $Z' = Z \Rightarrow \chi^{3'} = \chi^{3} = 0\chi' + 0\chi' + 0\chi' + \chi^{3}$
- N = N / Langley as dian x/1 - A.
- I continue to the second
0 0
is given by A. A. A. A.
$A_{j}' = A_{0}' A_{1}' A_{2} A_{3}'$
A. A. H. H.
Scanned with CamScan

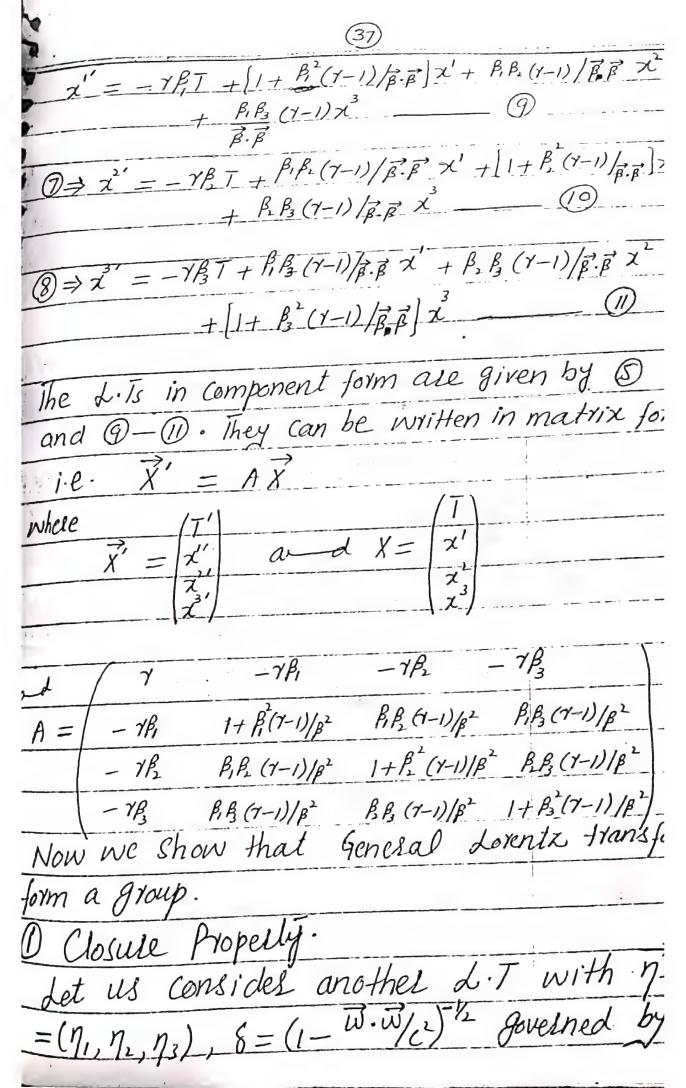




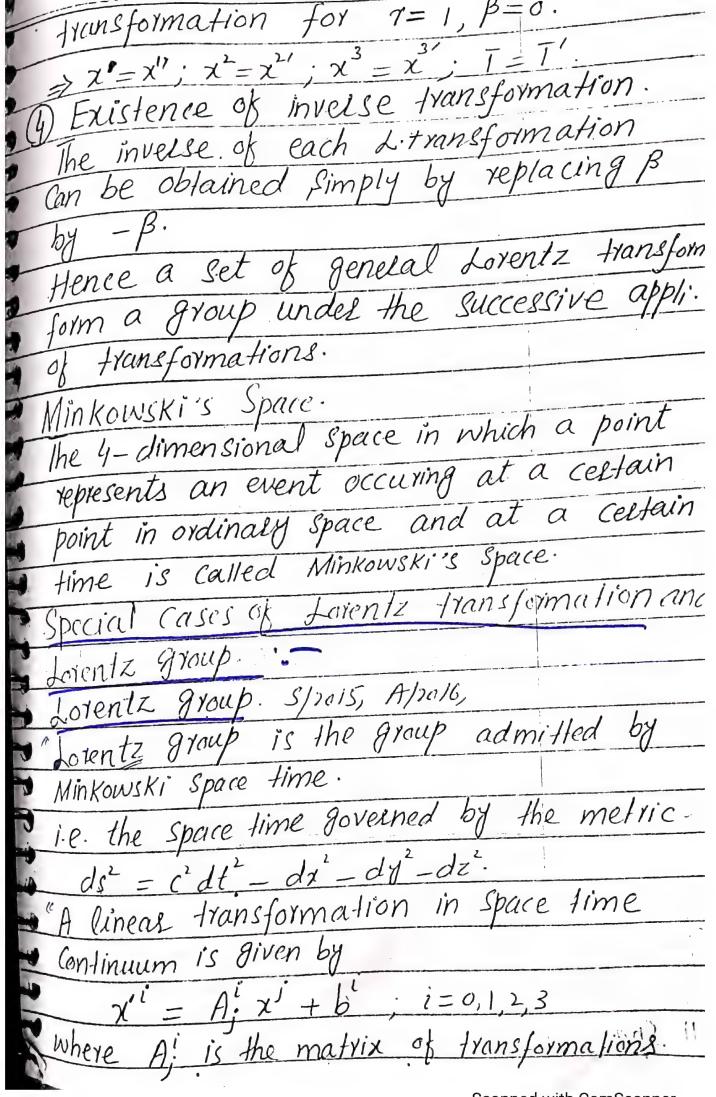
(38)
Sinhor Couches Sinhor
(0.0,0.
Guh (Cit Ci)
(ochlored) (ochlored) is give
- 1- (m) (8) (8) - 150) ((0))
The recultant of 100 many sinh (0,10,)
$= \int_{\mathbb{R}^{n}} \left(\frac{1}{x} \right) = \left(\frac{\cosh(\mathcal{O}_{1} + \mathcal{O}_{1})}{\sinh(\mathcal{O}_{1} + \mathcal{O}_{1})} \right) \left(\frac{1}{x} \right)$
(a) (Sinh(Site))
6.1
$\left(\begin{array}{c} T \\ X \end{array}\right)$
2' -1/6
$= i = \cosh\theta = \cosh(\theta_1 + \theta_2)$
$-7F = -\sinh\theta = -\sinh(\theta_1 + \theta_1)$
$\Rightarrow \beta = \sinh(\theta_1 + \theta_2) - \sinh(\theta_1 + \theta_2)$ $\cos h(\theta_1 + \theta_2)$
$= \frac{\sinh \theta}{\cosh \theta} = \frac{\tanh \theta - \tanh(\theta_1 + \theta_2)}{\cosh \theta}$
$\Rightarrow \hat{f} = \frac{\tanh \theta_1 + \tanh \theta_2}{\ln \theta_1} \qquad \therefore \beta_1 = \frac{\tanh \theta_1}{\ln \theta_2}$
- 1 + tanno 1 tanno B tanho.
$\Rightarrow \beta = \beta_1 + \beta_2$ $1 + \beta_1 \beta_2$
$\beta = V_{K}$
1+ 1/2 V2/c
$-1/V - (V_1 + V_2)^{1/C}$
1+ V1 V2/c2
⇒ V = V1+V2 which is relativistic law
1+ VIV2/c- of addition of velocities







The matrix $ -8\eta_{1} - 8\eta_{2} - 8\eta_{3} $ $ -8\eta_{1} - 8\eta_{2} - 8\eta_{3} $ $ -8\eta_{1} - 8\eta_{1} - 8\eta_{2} - 8\eta_{3} $ $ -8\eta_{1} - 8\eta_{1} - 8\eta_{2} - 8\eta_{3} $ $ -8\eta_{1} - 8\eta_{1} - 8\eta_{2} - 8\eta_{3} $ $ -8\eta_{1} - 8\eta_{2} - 8\eta_{3} - 8\eta_{3} $ $ -8\eta_{1} - 8\eta_{2} - 8\eta_{3} - 8\eta_{3} $ $ -8\eta_{1} - 8\eta_{2} - 8\eta_{3} $ $ -8\eta_{1} - 8\eta_{2} - 8\eta_{3} $ $ -11\eta_{2}(8-1)/\eta_{1}, \eta_{2} - 1+ \eta_{2}(8-1)/\eta_{3}, \eta_{3}(8-1)/\eta_{3}, \eta_{3}(8-1)/$
$B = \frac{1 + 11(8 - 1)\eta_{1}\eta_{2}}{\eta_{1}\eta_{2}(8 - 1)/\eta_{1}\eta_{2}} + \frac{1 + \eta_{2}(8 - 1)/\eta_{1}\eta_{2}}{\eta_{1}\eta_{2}(8 - 1)/\eta_{2}\eta_{2}} + \frac{1 + \eta_{2}(8 - 1)/\eta_{2}\eta_{2}}{\eta_{1}\eta_{2}(8 - 1)/\eta_{2}\eta_{2}} + \frac{1 + \eta_{2}(8 - 1)/\eta_{2}\eta_{2}}{\eta_{2}\eta_{2}} + \frac{1 + \eta_{2}(8 - 1)/\eta_{2}\eta_{2$
(n - 1/3-10-7-1
$\frac{1}{3}$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
-192 -193 9,93 (1-1) 17.0 9,93 (1-1) 17.0 1+43 (1
where $\overline{\Lambda} = (1 - \overrightarrow{u}.\overrightarrow{u})^{-1/2}$ and $\overrightarrow{u} = \overrightarrow{w} + \overrightarrow{\nabla}[(\overrightarrow{w}.\overrightarrow{v})/\overrightarrow{\nabla}.\overrightarrow{v}] - \overline{\Lambda}$ velocity
The Combination of Two Litransformations is itself a Litransformation.
DASSOCIATIVE Property. Now the associativity of matrices multiplication gamantees the associativ
Of L. Is. 3) Existence of identity transformation We nothe (T)
that $\begin{vmatrix} x'_1 \\ x'_2 \end{vmatrix} = A \begin{vmatrix} x''_1 \\ x''_2 \end{vmatrix}$ is an identity



W	
	wansformation given
	Iventa thans
	For every Lorentz transformation given; the matrix n; there exists an iden the matrix n; there exists the class
4	For lyix his relicios the class
	the matrix n; there he class the class element, invesse and satisfies the class element, invesse properly.
	econtactive property and all accession
	element, invesse and element, invesse propelly. and associative propelly. Thus forming a group under successive the sector of
11.	Thue forming a Transformation
å	I must be de do hese
4	Thus forming a group which is called Lorents admit a group which is called Lorents admit a group which by Lit
	- II a group which !
	aamin of Januted by Lil
	admit a group work by Lil group and is denoted by Lil The existence of invelse for any d.T The existence of invelse for that
	The existence the property that
	1. 0.0.0.7 1/9/ // //
	which is called critically the transformat
	However, the orthogonality of transformat
	magaze that to
4	$\frac{B = A_i^{\ell}}{B} \Rightarrow BB = I$
	$\frac{1}{1000} = \frac{1}{1000} = 1$
	$\Rightarrow BB^t = \overline{I} \Rightarrow BB^t = $
	$\Rightarrow B B^{t} = \Rightarrow B B = $
	$\Rightarrow 181^2 = 1 \Rightarrow 181 = \pm 1$
	The J.T. with 1B1 = +1 (or 1B1 = -1) is
	Called proper (or improper) L.T. The set
	all L.Ts forms a group which is subj
4	
	- of a group called Poincage group
1	Special Cases of L. To
-	Consider Some Special Cases of L.T.
	(1) Space-time rotations.

The d. Is given by x' = A; x reprents
space-time rotations.
The Sel of all such transformations form
a subgroup of Poincase group. This s-group
is called homogeneous L. group ar = simply
1. group which is denoted by L(6)/5
a Time Revelsal transformations:
1 Time Reversal transformations: The directs Obtained by replacing T by -T
(or t by -t) Such that
$T'=-T$, $\chi'=\chi$, $\chi'=\chi$, $\chi'=Z$
or d' = -d, x'=x, y'=y, Z'=Z
$\Rightarrow cdt' = -cdt$, $dx' = dx$, $dy' = dy$, $dz' = c$
$\frac{1}{2} \frac{C^2 dl'^2 - dx'^2 - dy'^2 - dz'^2}{2} = \frac{C^2 dl'^2 - dx'^2 - dy'^2 - dz}{2}$
ds' = ds'
The lineal transformation is the
It is called time reversel transformation and
this transformation interchanges past and fulure
It is to be noted that
11000
19ij = 0 -1 0 0 = -1
0 0 -1 0
0 0 0 -1 line reversed trans.
which shows that the time reversal trans.
is an improper transformation and is not
obtainable from the propel d. T.

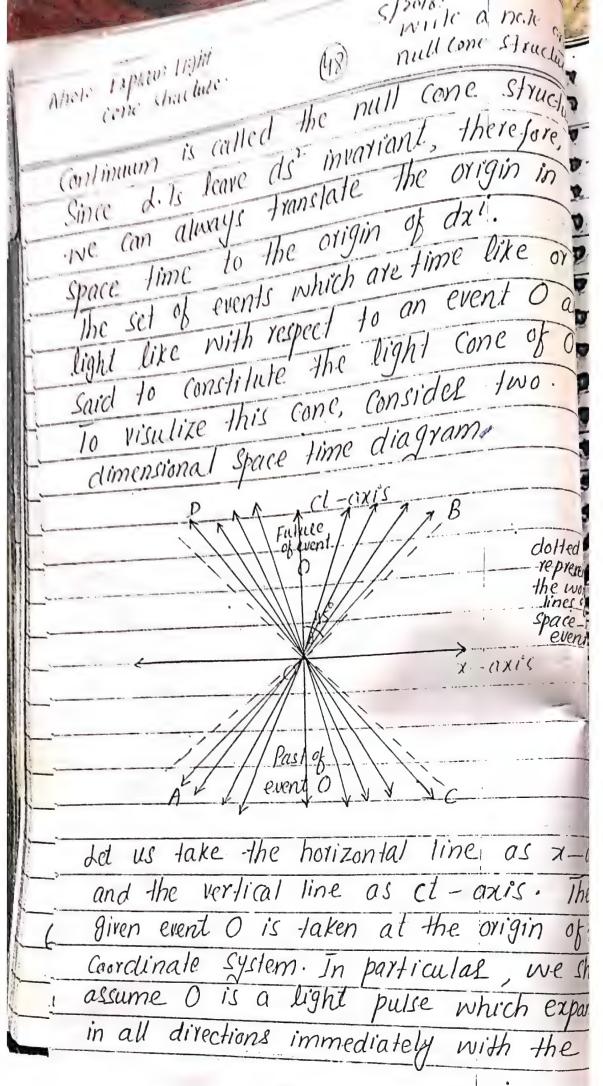
Note that the product of two time revertions formations i.e. $AB = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & -1 & 0 & 0 & 0 & -1 & 0 &$		42
transformations i.e. $AB = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & -1 & 0 & -1 \\ 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 0 & 0 & -1 $		ate that the product of two time rever
Ihus the time reversed transformations Thus the time reversed transformations a signal of transformation given by The transformation given by $x' = -x$, $y' = -y$, $z' = -z$, $t' = t$ which Changes the sign of every space to the equation. Coordinate and satisfies the equation. $x' = dx' - dx' - dy' - dz'' = c'dt' - (-dx) - c'dt' - dx' - dy' - dz'' = c'dt' - dx' - dy' - dz'' - $	11	ine. AB = 1000 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
Thus the time reverse a suggestion of the transformation given by The transformation given by $x' = -x$, $y' = -y$, $z' = -z$, $t' = t$ which changes the sign of every space to coordinate and satisfies the equation $x' = t' - t$		o o 10 identity mat
The transformation given by $x' = -x$, $y' = -y$, $z' = -z$, $t' = t$ which Changes the sign of every space to coordinate and satisfies the equation. $c'dt'' - dx'' - dy'' - dz'' = c'dt' - (-dx) - c'dt' - dx' - dy' - dz'' = c'dt' - dx' - dy' - dz'' - dz''$		a sugroup of L. group.
which Changes the sign of every space which changes the sign of every space is called space reflection. $ \begin{array}{cccccccccccccccccccccccccccccccccc$		- I was lies aller
Coordinale and satisfies.		$\chi' = -\chi$, $\eta' = -\eta$, $\chi $
is called space refrection of It is to be noted that (3) 8ij = 1000 v		Coordinale and satisfies $\frac{coordinale}{dz''-dy''-dz''} = c'dt'-(-dx)-c$
3 8ij = 1000 1 0 - 100 = -1		$\Rightarrow ds'' = ds''$.
Which shows that the space reflection	3	Jl is to be noted made 18ij = 1000
	#	which shows that the space reflection

is an improper liansformation and its not obtainable
Note that the product of two space reflection
Transformations
1000000000000000000000000000000000000
(ci) which is identity matrix.
-(8;) which is identity matrix. Thus the Space reflection transformations form a
Thus the spile refreshing than some
Space time translation
For A; = (8;) the unit matrix of
for A; = (o;)
ordes 4x4, reduces the equation
$\chi'' = \chi' + b'$; $i = 0, 1, 2, 3$.
gives us a set of transformations in 4-
dimensional space time and this transf.
Changes (x') - vector to a vector (x'i)
which is translation of vector (x') to
(11).
1 de aglarma light dom a dioup of 9-
Poincase' group: - A/2013. S/2015 Poincate group
Paiacare' group A/2013. S/2015 Poincale' group
- I and i've grow what which prings
The state of the s
is the ten parameter Poincare' group.
is the ten parameter to T(4)
i.e. P(10) = L(6) &) T(4)
The state of the s

(44)
1 (6) denotes the proper Lorent the
= Table the Miland
where L(b) denotes the
White I the little of the partial last
group with the votations,
where L(6) the number 6 de spatial 10, group and the number 3 for spatial 10, number of rotations, 3 for spatial ion. number of rotations, 3 for spatial ion. Translation
number of rotations, 3 lor rotation. number of rotations, 3 lor rotation. number of rotations, 4 temporal rotation. and 3 for spatial temporal translation the group of translation
number of rotation temporal rotation and 3 for spatial temporal translation and 3 for spatial temporal translation of translation (4) denotes the group of on four particles depending on four particles depending on four particles.
and 3 for specific group of on four parties of 4-vectors depending on four parties that the element and 8 indicates that the with T(4).
of 4- vector that the
L(6) do not commute considering This may be seen by considering
This may be seen of
$\frac{as}{x'^i} = A^i_i x^j$
2
and then
$\chi'''\dot{i} = \chi' + b$ $= \lambda^{i} \chi^{j} + b^{i}$ $= \lambda^{i} \chi^{j} + b^{i}$
$=A; \chi^{0} + 0$
$\Rightarrow x''' = A'_{1}x' + b'_{2}$ The other hand if we define
on the other hand if we don't
$\frac{1}{x^i} = x^i + b^i$
1 then
AL XI
$\frac{2^{x} = \eta_{j}(x^{i} + b^{i})}{2^{x}} using 0$
$\frac{0}{3} \Rightarrow \dot{x}^i = A^i_i \dot{x}^i + A^i_i \dot{b}^i$
Find (9), we have
1 1011
7/1. I at valations in n-am
The group of rotations

N/2012, Classify the interved
Heri, lise Din the place (46)
Heri, lise Din the classified into
1.6 191(0)1
A vector de meg following three categories.
-following Three vector 1/2018
- following me like vector Define
(i) Time like vector Define (ii) Null / light like vector (ii), (ii), (ii), (iii), (iiii), (iiii), (iiii), (iiii), (iiii), (iiiii), (iiii), (iiiiiiiiii
(iii) Space like vector. A/2009
(iii) Space like vector. A/2009 (i) Time like vector. A/2009
The 4-vector dx is called time like
$\frac{ds^2>0}{ds^2>0}$
$\Rightarrow c^2 dt^2 - ds^2 > 0$
$\frac{\Rightarrow c^2dt - uz}{\text{where } dz^2 = dz^2 + dy^2 + dz^2}$
$\Rightarrow c^2 dt^2 > ds^2$
> c2 > d1
08/d8/ LC.
dt
=> the Spatial distance between tw
Can be coveled with velocity less than
velocity of light.
Thus, for time like vectors the ma
of velocity V is less than C. 1h
- of verocity vericent the actual path
dxi can represent the actual path
physical object in space over time
(a Speed ds LC.
dt A/2009,
(ii) Null vector Light like vector.
A 4- vector dzi is called null

(47)
like vector if $ds^2 = 0$
$\Rightarrow c^2 dt^2 - ds^2 = 0$
$=\frac{1}{2}e^{2}dt=ds^{2}$
$\Rightarrow c' = d\vec{x} ^2$
dt
$\Rightarrow C = d\vec{x} \Rightarrow c = d\vec{x}' $
For anull vector the magnitude of V
is equal to c.
Thus dxi can represent the path of a
physical object travelling at a light speed.
(iii) Space Like vector. A/2009, A/2012
A 4- rector dx' is called space like
vector if ds 20.
$\Rightarrow C^2 dt^2 - ds^2 \leq 0$
$\Rightarrow c^2dt^2 \leq ds^2$
\Rightarrow $C^2 \leq d\vec{s} ^2$
di
$\Rightarrow d\vec{s} > c$.
For a space like vector, the magnitude of
is greates than C, which is not possible.
for a physical object such as a particle.
We can represent all the three types
of vector together graphically. This graphical
representation of 4- vector in space time



Speed C. Thus, in Space-time diagrama the distance covered by the light particle is x = ct $\frac{\Rightarrow z}{ct} = 1 = +anys$. We draw this line and call it AOB is the world line of a particle which moves with speed c and this world line makes an angle 0=45° with ct-axis. The same is true about the world line COD. Thus any event on these lines AOB and COD is light like. Since a material particle would always be moving with velocity vzc, therefore, its world line will make an angle less than 450 about ct - axis. So the motion of a material particle will always a represented by a line lying in the sectors AOC and BOD. All the events in sector AOC will be in the past of event 0 and all the events in sector BOD will be in the future of event 0. The sectors BOC and AOD represent the world lines of the particles which moves with velocity V'>C. The events in these

1	(50)
	regions Boc and AOD are said to be
Carried And	regions Boc and 1100
	remole. The three space
	If we consider all the three reginal coordinates (x, y, z), then the three reginal coordinates (x, y, z) absolutely remote of
	of past, future and absolutely remote of
	Sparaled by the hypercone in the 4-dim
	Sparaled by the inflore space The axis of this hypercone cointing
	with ct -axis.
	This hypercone is called light cone !
	Cone. Fis
	Absolute
	Absolute Absolute remot
-	hbsolute past
	Expression for proper time as an
-	integral.
	Consider the invariant interval ds in
·	rest frame of the observes O.
4	Then $ds^2 = C^2 dt^2 - dx^2 - dx^2 - dx^2$
	for all observes in yest frame
	$dx' = (dx', dx', dx^3) - (0.00)$
	then $0 \Rightarrow ds' = c' dt'$

(5i) > dī = ds/c2 $\Rightarrow d\bar{t} = ds/c$ is an invariant quantity Now an observer in S' frame measures the time dt' and the spatial displacement d?" and obtains the invariant quantity as $\frac{ds'^{2}}{ds'^{2}} = c^{2}dl'^{2} - dx'^{2} - dy'^{2} - dz'^{2}$ $\Rightarrow ds'^{2} = c^{2}dl'^{2} - (d\vec{x}')^{2}$ But $ds'^{2} = ds^{2}$, then $ds^{2} = c^{2}dl'^{2} - (d\vec{x}')^{2}$ Substituting 2 in 3, we get $c^{2}dT^{2} = c^{2}dt^{2} - (ds^{2})^{2}$ $\Rightarrow dt^{2} = dt^{2} - 1 (u^{2}dt^{2})^{2}$ $= dt' - \frac{1}{2} u' dt'$ $= (1 - u'^{2}) dt'^{2}$ > dt = /1-u'/2 dt Integrating, we get · = [] 1-u', dl' which is the expression for proper time as measured by the moving observel;

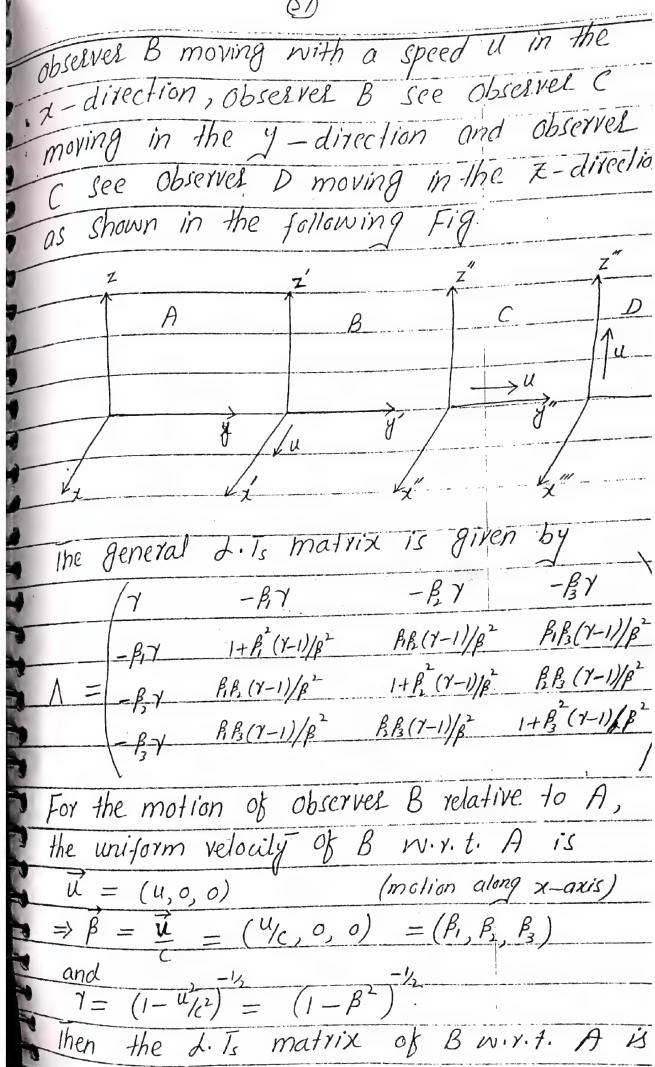
2 N/2014
Framples. 1/2009, 1/2014 The vectors T, X, Y, Z are given by [1] y a = (0,1,0,0); y a = (0,0,0);
The vectors 1, x, y, z are
$T'' = (1,0,0,0)$, Λ if the only vanishing
The vectors T , X , Y , Z are 0^{11} . $T^a = (1, 0, 0, 0)$, $X^a = (0, 1, 0, 0)$; $Y^a = (0, 0, 0)$ $Z = (0, 0, 0, 1)$. Show that the only vanishing $Z = (0, 0, 0, 1)$. Show the vectors are inner products believe the vectors are
7 7 = 1.
innel Products occurred in the product of the products occurred in the product of the products occurred in the product of the
Define $L^a = \frac{1}{L}(1+L)$, $\frac{1}{Ma} = \frac{1}{L}(X^a - iY^a)$
Define $L = \frac{1}{\sqrt{1 + iy^a}}$ and $M = \frac{1}{\sqrt{1 + iy^a}}$
Ling Ma and Mas vectors, Show That
the tall vectors are null and city
vanishing inner products La Na = - Ma Ma=
Solution.
As we know that
$T' = \theta_{ab} T^{a} T^{b} = T^{a} (\theta_{ab} T^{b}) = T^{a} T_{ab} T^{b}$
$\Rightarrow T^{2} = T^{0}\overline{I_{a}} \qquad = 0$
$\int \frac{\sin a }{x^2} = \frac{x^a}{x^a} = \frac{x^a}{x^a$
$\frac{y^2 - y^0 y_0}{y^2 - y^0} = 3$
$\frac{Z^2 - Z^a Z_a}{In Min Kowski' Space} $
$\frac{2h}{ds^2 = c^2dt^2 - dx^2 - dy^2 - dz^2}$
$\Rightarrow \theta_{00} = 1, \theta_{11} = \theta_{22} = \theta_{33} = -1 \theta_{24} = 0$
$\Rightarrow T = g_{00}(T^{0})^{2} + g_{11}(T^{0})^{2} + g_{12}(T^{0}) + g_{33}(T^{0})$
U100-1-1 (12) 1 (133 17)

 $-(0) - (0)^2 - (0)^2 = 1$ (7°) is a time like vector. X = gab X a X 6 $= g_{00}(X^{0})^{2} + g_{11}(X^{1})^{2} + g_{21}(X^{2}) + g_{33}(X^{3})$ (0)' + (-1)(1)' - 1(0)' - 1(0)' $X = (X^{\circ})$ is a space like vector. Y'= gab yayb $= g_{00} (\gamma^{0})^{2} + g_{11} (\gamma^{1}) + g_{21} (\gamma^{1}) + g_{33} (\gamma^{3})$ $1(0)^{2} - 1(0)^{2} - (1)(1)^{2} + (-0)(0)$ Y=(Y°) is a space like vector. Z'= gab ZaZb $= \theta_{00} (z^{\circ})^{2} + \theta_{11}(z') + \theta_{22}(z') + \theta_{33}(z')$ $= 1(0)^{2} - 1(0)^{2} - (1)(0)^{2} - 1(1)^{2}$ => Z=(z°) is a space like vector. $T^{2} - \chi^{2} = -\chi^{2} = -Z^{2} = 1. \quad \chi^{2} = (c, 1)$ $M' = g_{ab} M^{a} M^{b} M^{a} + (x^{a} - iy^{a})$ Mon $= \theta_{\infty}(M') + \theta_{11}(M') + \theta_{11}(M') + \theta_{21}(M') + \theta_{22}(M')$ $=(1)(0)^{2}+(-1)(\frac{1}{2})^{2}+(-1)(\frac{1}{2})^{2}+(-1)(0)$

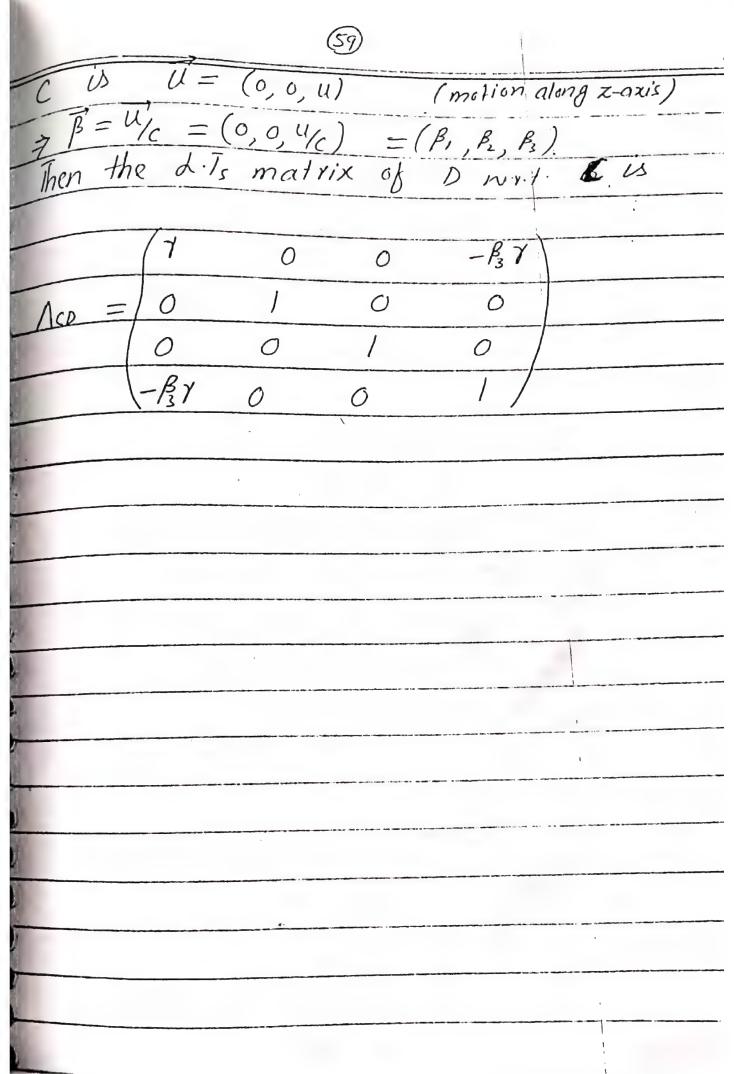
 $-\frac{1}{2} - (-\frac{1}{2}) = -\frac{1}{2} + \frac{1}{2} = 0.$ $\frac{A^{2} = 0}{A^{2} = 0}$ $\frac{A^{2} = 0}{A^{2} = (M^{0})} \text{ is a null vec-lor.}$ $\frac{A^{2} = \theta_{0b} N^{0} N^{0}}{A^{2} = \theta_{0b} N^{0} N^{0}} + \theta_{11}(N') + \theta_{21}(N') + \theta_{32}(N')$ $= \theta_{00}(N^{0})^{2} + \theta_{11}(N') + \theta_{21}(N') + \theta_{32}(N')$ $= (1)(\frac{1}{\sqrt{2}})^{2} + (-1)(0)^{2} + (-1)(0)^{2} + (-1)(-1)(-1)^{2}$ N= (N°) is a null vector. L= gab La Lb = 800 (L°) + 811 (L') + 822 (L) + 833 (L) $= (1)(\frac{1}{2})^{2} + (-1)(0)^{2} + (-1)(0)^{2} + (-1)(\frac{1}{2})^{2}$ null - vector, and $= \theta_{00}(M^{\circ})^{2} + \theta_{11}(M^{\prime}) + \theta_{12}(M^{2}) + \theta_{33}(M^{3})$ $(1)(0)^{2}+(-1)(\frac{1}{2})^{2}+(-1)(-\frac{1}{2})^{2}+(-1)(0,$ null vector. tast finally, we find and " Using eq, (1

```
= 800 (L°)(N)+ 811 L' N' + 922 L' N' + 933 L3N3
  = (1)(\frac{1}{2})(\frac{1}{2}) + (-1)(0)(0) - 1(0)(0) - 1(\frac{1}{2})(\frac{1}{2})
 = - - 0 - 0 + / = 1
> L Na = 1.
and M^a M_a = g_{ab} M^a M
      = 800 M°M° +811 M'M +822 M'M + 933 MM
      = (1)(0)(0) + (-1)(\frac{1}{2})(\frac{1}{2}) + (-1)(\frac{1}{2})(-\frac{1}{2}) - 1(0)(0),
      = -\frac{1}{2} - \frac{1}{2} = -\frac{1}{2}
 = \sqrt{M^a M_a} = -1 or -M^o M_a = 1
  Hence L'Na = - Ma Ma = 1.
 Example 2. A/2018 \Rightarrow X^{\alpha} = (0,0,1,0), Y^{\alpha} = (2,1,0,1), Z = (1,1,0,1)
  classify the following vectors as time-like,
   null. or space-like.
    A^{\alpha} = (-1, 4, 0, 1), B^{\alpha} = (2, 0, -1, 1)
   and C^a = (2, 0, -2, 0)
  Solution.
   Given that
    A^{a} = (A^{\circ}, A', A, A') = (-1, 4, 0, 1)
    B^{a} = (B^{a}, B', B', B') = (2, 0, -1, 1)
  C^{\circ} = (C^{\circ}, C', C^{\dagger}, C^{\dagger}) = (2, 0, -2, 0)
  Therefore,
     A= Pab AAA
       = 900 (A°) + 911 (A') + 922 (A) + 933 (A3)
```

In Minkowski space $ds^2 = c^2 dt^2 - dx^2 - dy^2 - dz$ $\frac{1}{1} \frac{\partial}{\partial s} = \frac{1}{1} \frac{\partial}{\partial s} = \frac{1}{1} \frac{\partial}{\partial s} = \frac{1}{1} \frac{1}{1} \frac{\partial}{\partial s} =$ $= 1 - 16 - 1 = -16 \angle 0$ $\Rightarrow A = (A^{\circ}) \text{ is a space like Vector.}$ $B^{2} = g_{00}(B^{0})^{2} + g_{11}(B^{\prime})^{2} + g_{12}(B^{\prime})^{2} + g_{33}(E)$ $= 1(2)^{2} - 1(0)^{2} - 1(-1)^{2} - 1(1)$ = 4 - 1 - 1 = 2 > 0 $\Rightarrow B = (B^{\circ}) \text{ is a time like vector.}$ and $C' = g_{00}(C')^2 + g_{11}(C')^2 + g_{22}(C^2)^2 + g_{33}(C^3)^2$ = $1(2)^2 - 1(0)^2 - 1(-2)^2 - 1(0)^2$ $= \frac{4-4}{2} = 0$ $\Rightarrow C = (C^{\circ}) \text{ is a null vec-loy.}$ Problem.Let an Observer A see Observer B mov with a Speed u in the z-direction, obs See Observer C moving in the Y-direct and observes C see observes D moving the Z-direction. Work out the L.Ts m of the motion of D relative to A ar of A relative to D. Are the two ma inverses of each other? Solution. Let us assume that an observer A

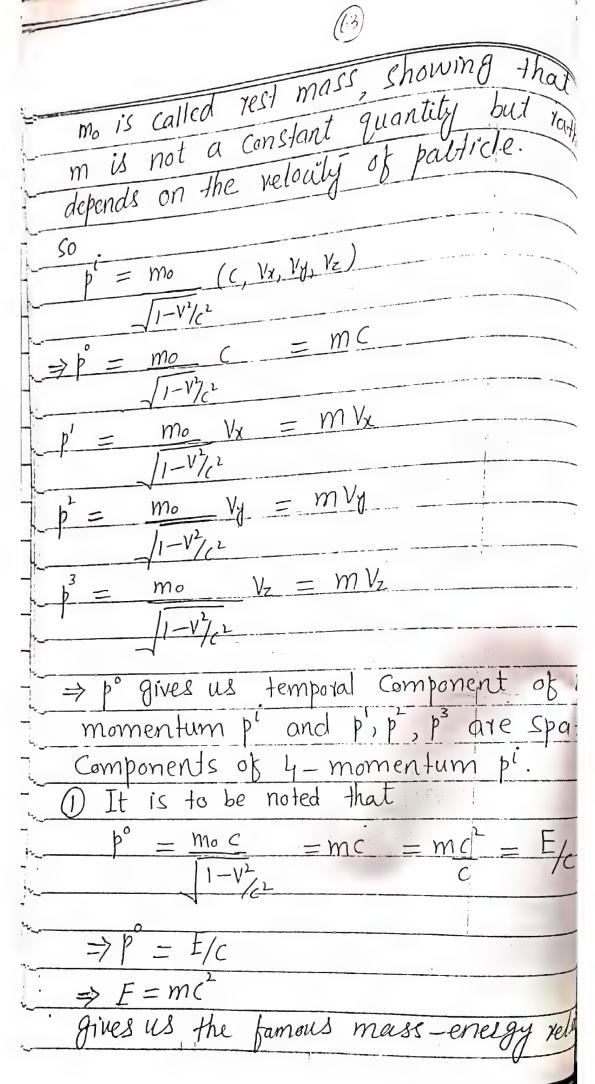


(58)
-BY
$-\beta_{1}\gamma + \beta_{1}^{2}(\gamma-1)/\beta^{2} = 0$
$-\beta_1 \gamma + \beta_1 \gamma - \gamma \beta_2$
$\Delta_{AB} = \begin{array}{c} -p_{II} \\ 0 \\ 0 \end{array}$
where $\frac{1+\beta_{1}^{2}(\gamma-1)/\beta^{2}}{1+(\gamma \delta-1)} = \frac{1+\frac{u^{2}(\gamma-1)}{u^{2}(\gamma-1)}}{1+(\gamma \delta-1)}$
whele 1+ P1 (7-1)/B - 1 + (76-1)
$= \frac{1}{1}$
$\Rightarrow 1 + \beta^{+}(\gamma - 1)/\beta^{+} = \gamma$
$= \frac{1}{1} $
$\Rightarrow \Lambda_{AB} = \begin{vmatrix} -\beta_1 \gamma & \gamma \\ 0 \end{vmatrix}$
0 0
0 0 0
For the motion of observed C ret
to B, the uniform velocity of [wi
$\vec{u} = (0, u, 0)$ (motion along y-ar
$\Rightarrow \vec{\beta} = \vec{U}_{c} = (0, U_{c}, 0) = (\beta_{1}, \beta_{2}, \beta_{3})$
Then the L. Is matrix of C wirt. BU
1.7 0 -BY 0
$\Delta BC = 0$ 1 0 0
-BY 0 7 0
£ 0 0 1 1
-! Similarly, for the motion of observel
relative to C, the uniform velocity of



y L
$\frac{1}{1} \frac{1}{1} \frac{1}$
dit = (1)
at'
· dt - 7.
=> (11 = 1
cll
Note that
1dx dy dz = dt dt dt di
di di di
- (V1, V1, V2) 7
$\frac{7}{2} \frac{7}{2} \frac{7}$
Substituting (2) and (3) in (1), we get
The squared magnitude of four-velocity
is given by
$V^2 = g_{ij} V^i V^j$
$= 900 (V^{\circ})^{2} + 911 (V') + 912 (V') + 933$
In Minkowski space, we have!
$g_{00} = 1$, $g_{11} = g_{22} = g_{33} = -1$
Thus
$V^{2} = (1)(\gamma_{C})^{2} + (-1)(\gamma_{V_{x}}) + (-1)(\gamma_{V_{y}}) + (-1$
$= 7^{2}c^{2} - \gamma^{2}(V_{x}^{2} + V_{y}^{2} + V_{z}^{2})$
$= \gamma^2 c^2 - \gamma^2 V^2$
$= \gamma^{2}C(1 - V/C^{2}) = \gamma^{2}C^{2}\gamma^{-2}$
$\Rightarrow V^2 = c^2$
The 4-velocity vector V' = (v, V, V, V)
tyon (toyand in the
The same way as the
Scanned with CamScann

```
position 4- vector
                   \chi' = (\chi', \chi', \chi', \chi')
        = \gamma(x-vt) = \gamma(x -
             \gamma(\chi'-\chi\chi^\circ)
               ; Z'= Z
                V^3 = V^3
 -momentum: - Aprois
  us consides a particle in motion. Let V'
be its 4- velocity. Then the product of the
Velocity 4- vector with a 4- scalar mo is
        4-vector and is called 4-momentum
                 = m_o(V^\circ, V, V, V^*)
       = moV
                = m_o(7C, 7\vec{V})
                 = mo7 (C, Vx, Vy, Vz
det us introduce m= mor =
which is called the
 relativistic mass, dependent
       velocity of the moving obje
on the
```

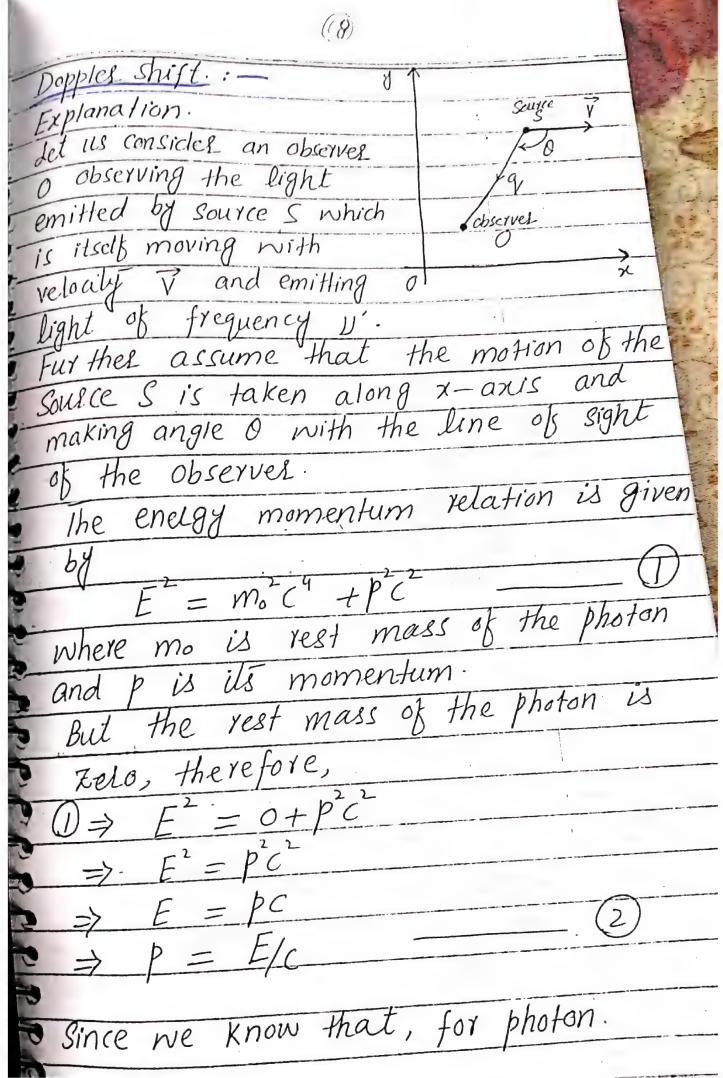


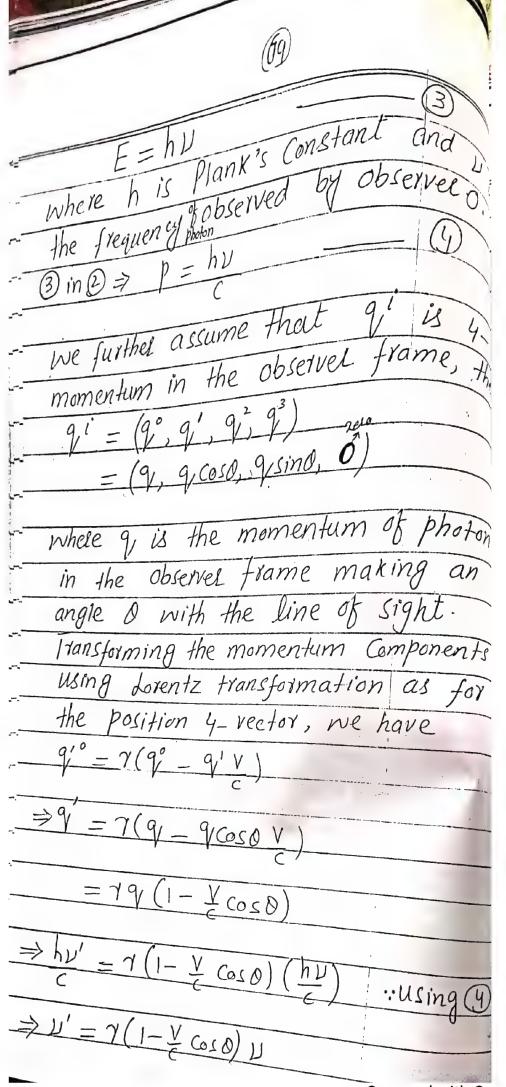
$(\underline{C},\underline{Y})$
10
and $p^{\circ} = m_{\circ} c = m_{\circ} c^{\circ} \perp E_{\circ}$
$\sqrt{1-v^2/c^2}$ $C/1-v^2/c^2$ $C/1-v^2/c^2$
7-16
22-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-
=> Eo = moc' is called rest mass enelgy
or residual energy.
@ Also note that the K.E. of the particle
Casa Qiyan by
in this case given by
$T = E - E_0$
$=mc^2-m_0c^2$
/ 1/4/
= mo7c2 - moc ": y=/1-1/c2
$= m_0 c^2 (\gamma - 1)$
$= m_0 c^2 (\gamma - 1)$ $= m_0 c^2 \left[(1 - V^2)^{-1/2} - 1 \right]$
$=\frac{1110C}{C^2}$
$\frac{2}{\sqrt{1 + (1 + \sqrt{3})}} \frac{1}{\sqrt{1 + (1 + \sqrt{3})}} \frac{1}{\sqrt{1 + \sqrt{3}}} \frac{1}{\sqrt{1 + \sqrt{3}}}} \frac{1}{\sqrt{1 + \sqrt{3}}} \frac{1}{\sqrt{1 + \sqrt{3}}}} \frac{1}{\sqrt{1 + \sqrt{3}}} \frac{1}{\sqrt{1 + \sqrt{3}}}} \frac{1}{\sqrt{1 + \sqrt{3}}} \frac{1}{\sqrt{1 + \sqrt{3}}} \frac{1}{\sqrt{1 + \sqrt{3}}}} \frac{1}{\sqrt{1 + \sqrt{3}}} \frac{1}{1 + \sqrt$
= $m_0 C^2 \left[\left(1 + \frac{1}{2} \right)^2 \left(2^2 + \left(-\frac{1}{2} \right) \left(-\frac{3}{2} \right) \right]^{\frac{1}{2}} \right] = \frac{1}{84} Binon$
And the state of t
$\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)\sqrt{\frac{6}{6}}+\cdots\right)-1$ expansion.
31
$\frac{1}{2}$
$= m_0 c^2 \left(\frac{V_2^2}{2c^2} + \frac{3}{8} \frac{V_4^4}{\sqrt{c^4}} + \frac{5}{16} \frac{V_6^6}{\sqrt{c^6}} + \cdots \right)$
$= \frac{1}{5} m_0 V^2 + \frac{3}{8} m_0 V^4 + \frac{5}{16} m_0 V^6 + \cdots$
2 8 C2 16 C4
2(, 2 \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \
$= \frac{1}{2} m_0 V^2 \left(1 + \frac{3}{4} V_{c2}^2 + \frac{5}{8} V_{c4}^4 + \cdots \right)$
FOY V ZZ C, /c >0, V/cz >0, V/cz
and so on.

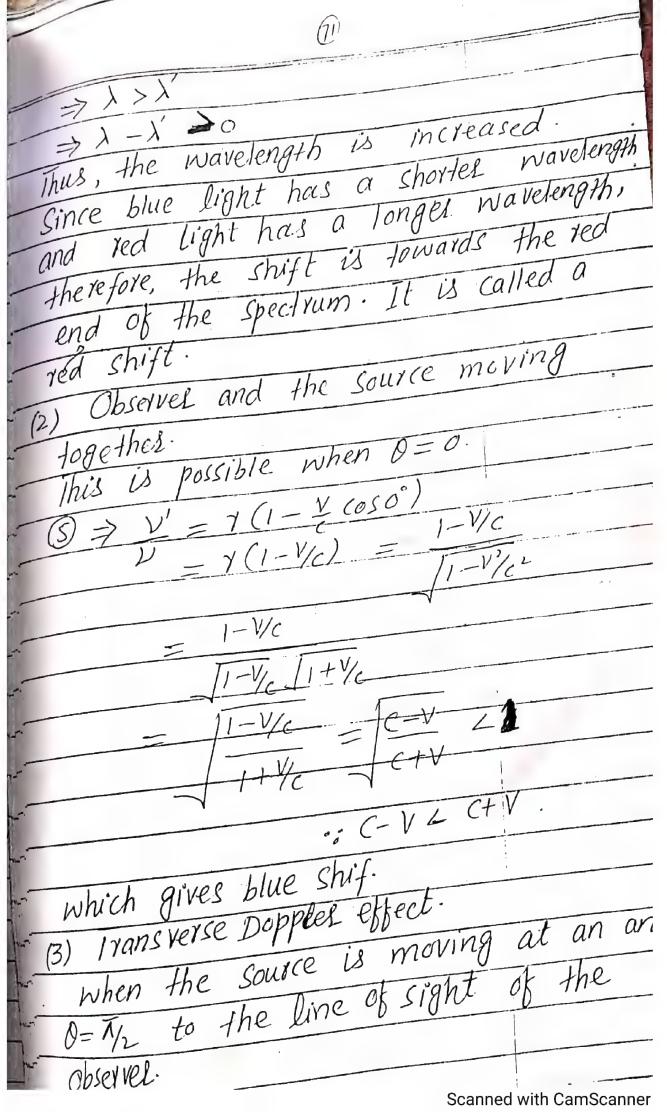
represents classical Newtonian limit Hence, $T = \frac{1}{2} m_0 V^2$ The relativistic Correction to classica relativistic result. expression for K.E. is given by $\frac{7-1}{2c^{2}} = \frac{(1-\frac{V_{c}^{2}}{2})^{-1/2}}{2c^{2}} = \frac{1+\frac{V^{2}}{2}}{8} = \frac{3}{6} = \frac{4}{6} = \frac{4}{6} = \frac{1+\frac{V^{2}}{2}}{8} = \frac{3}{6} = \frac{4}{6} = \frac{1+\frac{V^{2}}{2}}{8} = \frac{1+\frac{V^{2}}{2}}{8} = \frac{3}{6} = \frac{1+\frac{V^{2}}{2}}{8} = \frac{1+\frac{V^{2}}{2}}$ $=\frac{V^{2}}{2c^{2}}+\frac{3}{8}\frac{V^{4}}{c^{4}}+O(\frac{V}{c})$ which yields = (7-1) m. c2 $\left[\frac{V^{2}+3}{2C^{2}}+\frac{3}{8}\frac{V^{4}+0(\frac{V}{c})^{6}}{(\frac{V}{c})^{6}}\right]$ moc² $= \frac{1}{2} m_0 V^2 + \frac{3}{8} m_0 V^4 + 0 (V/c)^4$ = 1 mov2 (1+3 v/c2+0(1/c)4 we take m instead of mo, then = (7-1) moc = $(\gamma-1)$ $m_0\gamma$ $(^2$: m= m08

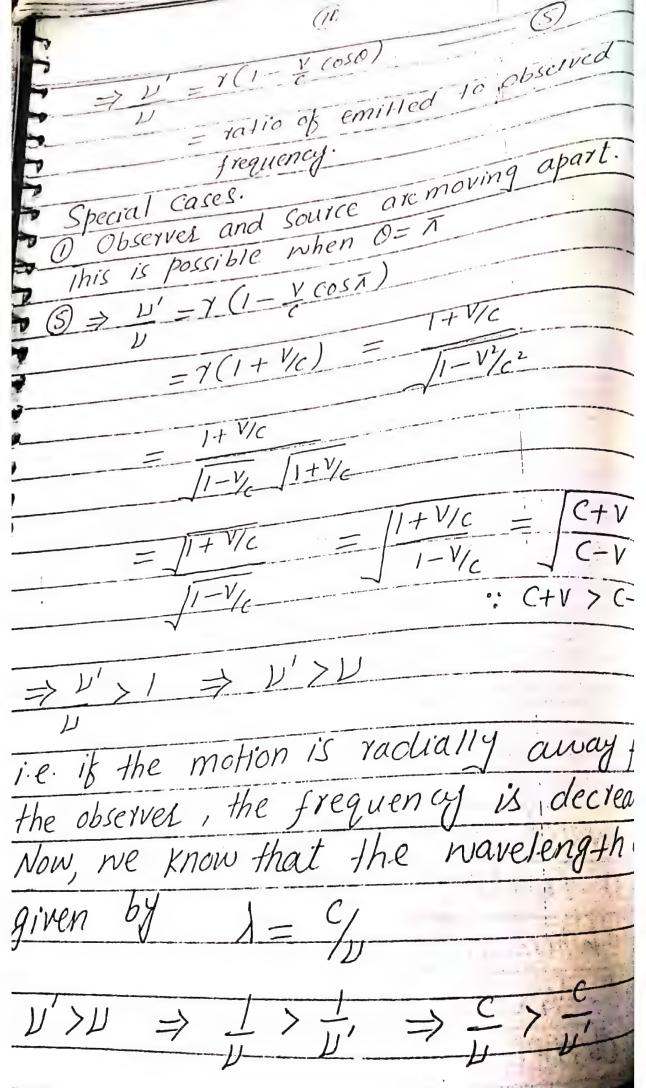
=/ 1 = (1-7-1) rnc = 11-(1-1/2) 11/2 $= \left[1 - \left(\frac{1}{2} + \frac{1}{2} + \frac{1}$ $\left(\frac{1}{2} + \frac{1}{6} + \frac{$ $= \frac{1}{2} m v^{2} (1 + \frac{1}{4} v/c^{2} + o(v/c)^{4})$ Where m= mor is relativistic mass. The squared magnitude of 4-momentum in Minkowski Space is $= g_{00} (p^{0})^{\frac{1}{2}} + g_{11} (p^{\prime})^{\frac{1}{2}} + g_{21} (p^{\frac{1}{2}})^{\frac{1}{2}} + g_{33} (p^{3})^{\frac{1}{2}}$ $= (p^{0})^{\frac{1}{2}} - (p^{\prime})^{\frac{1}{2}} - (p^{2})^{\frac{1}{2}} - (p^{3})^{\frac{1}{2}}$ p'= gi; pi ps $(m v_x)^2 - (m v_y)^2 - (m v_z)^2$ m'c2 - m2(Vx + Vy + Vz) - m2 V2 : m = m. 8. A/20 A/2013, A/20 Energy Momentum relation. A/2009, A/2010 The energy momentum relation can be observed from squared magnitude of 4-momentum in Minkowski Space.

8	
	$(b^3)^2$
p - girli	12-(1)
1092 - (1)	7 7
	p = E/c
1 m 2 2 = (p)	
1	
F/2 - P	
= 1/C pc	
1 2 h	, 2
== PC	12. 2
) 4 1	PC
	red energy momen
POTOC	
relation.	nontum Components
Sd. Ts for 4-mor	mentally corrects
flat p' and p'	be the 4- momentu
in the two coordi	nate system, then the
L. To Connecting pl	and p'i is given b
$p'^{\circ} = \gamma (p^{\circ} - p' \vee p')$	· · · · · · · · · · · · · · · · · · ·
C	
$-\frac{p''}{}=7(p'-\underline{V}p^\circ)$	
h'2 - h'2	3 ,3
	= p.
Dobples alich	
Dopples Shift in K	elativily. S/2018.
1111/1/	
and observes in	Called the relation
	caused the relation
	Scanned with CamScann



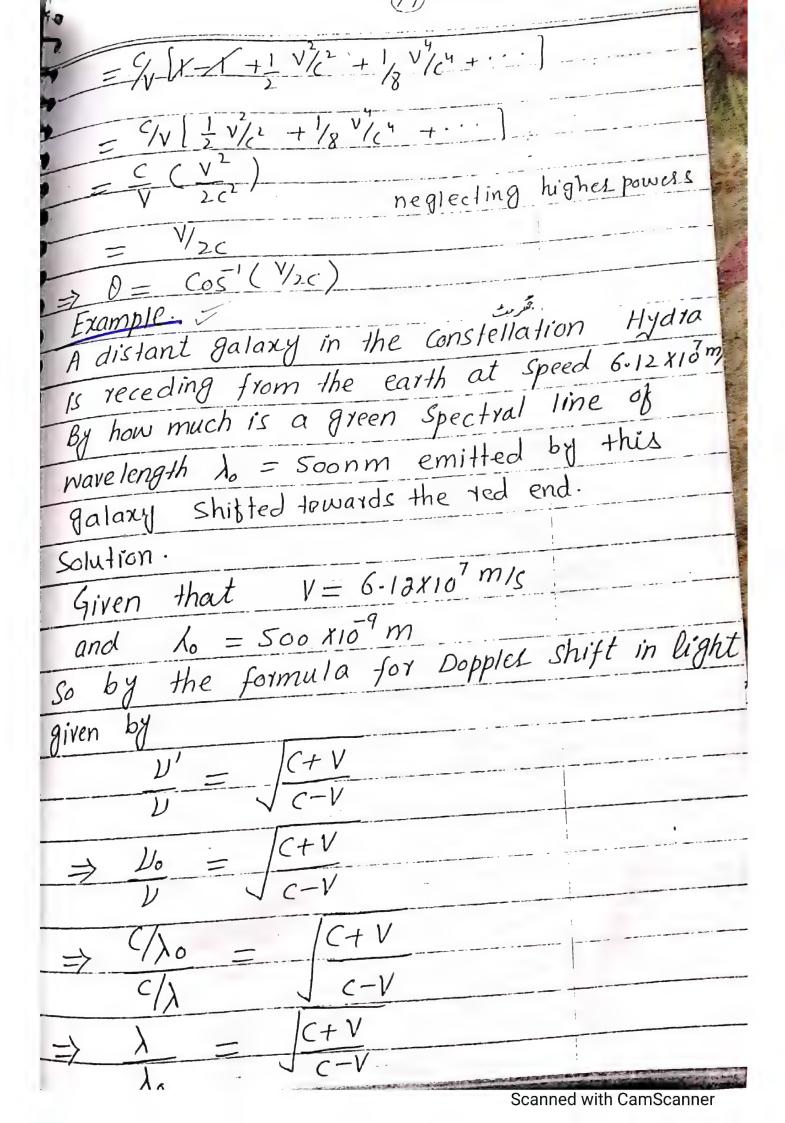


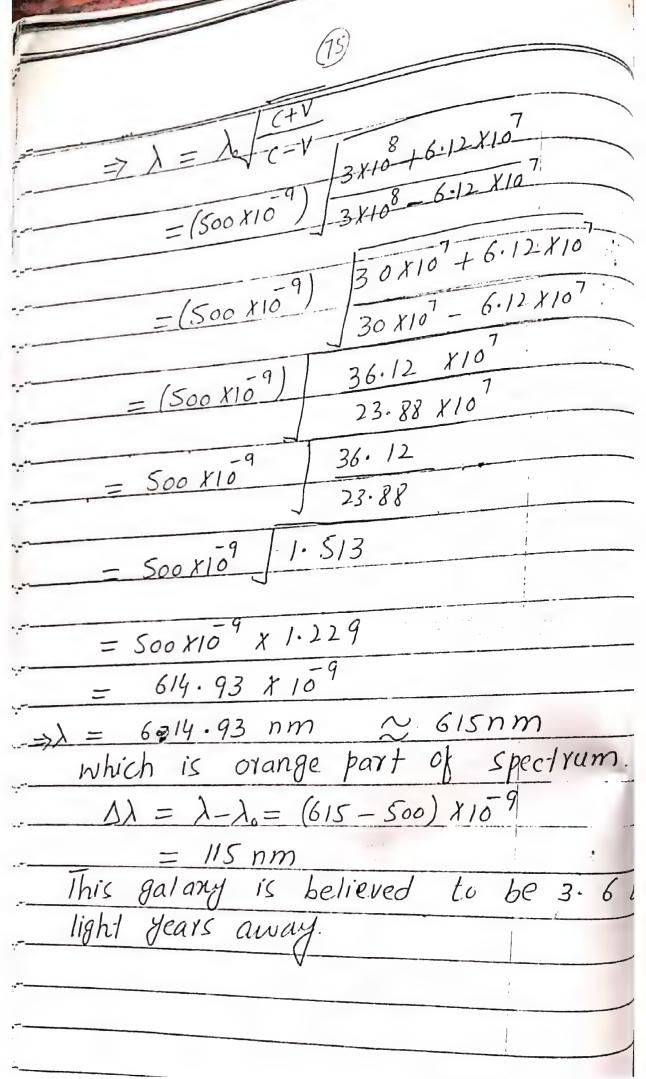




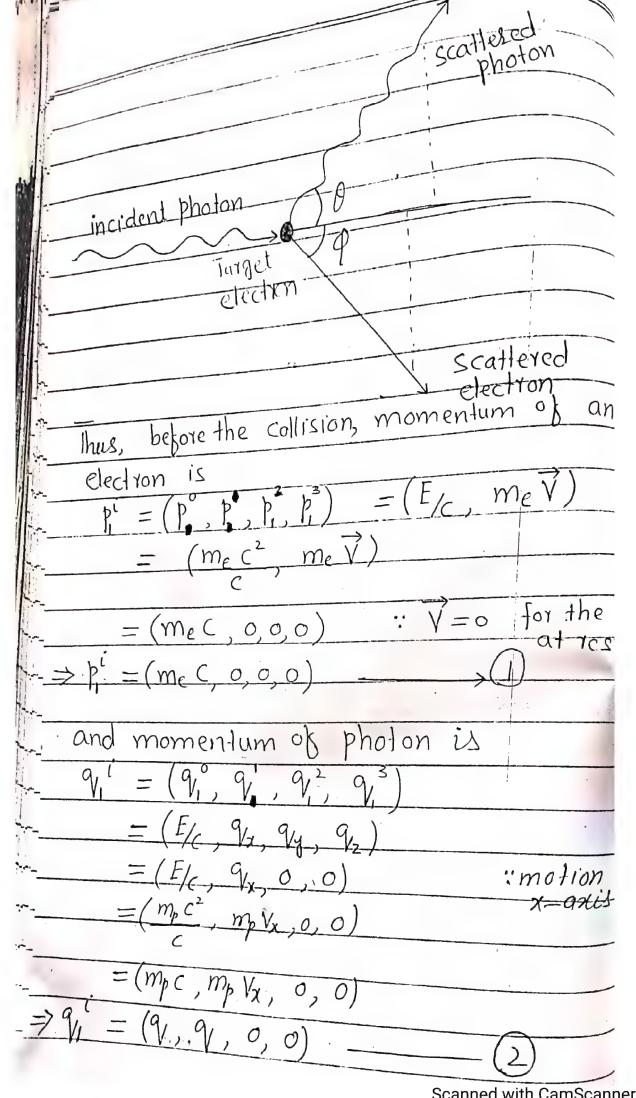
Then (5 => 1 = 7 (1 - 2 cos x) $\Rightarrow \frac{y'}{y} = \frac{1}{|1-v'|_{C^2}}$ which is due to time dilation. (4) Condition for no Doppics Shift. Let us find o for which there is no Doppler Shift. i.e. U'=U. Subsituting (5) in (2), we get $\gamma(1-\frac{1}{2}(000))=1$ $\Rightarrow 1 - \frac{V}{c} \cos 0 = \sqrt{1 - \frac{V_{c2}^2}{2}}$ On Squaring, we get $(1-\frac{1}{2})(\cos \theta)^2 = 1-\frac{1-\frac{1}{2}}{2}$ => 1+ V2 (050 - 2 V (050 = 1 - V/2) => $\frac{1}{V^{2}} \frac{V^{2}}{COS^{2}O} - \frac{1}{2} \frac{V}{COSO} - \frac{1}{V^{2}} \frac{V^{2}}{C} = 0$ $\Rightarrow \frac{V^2}{COSO} - \frac{\partial V}{\partial V} \cos O + \frac{V^2}{COSO} = 0$ which is quadratic equation in coso.

[13]
By quadratic formula, we have
By quadratic formula, vocal (v/c2)
01/ 7/1/
(OSO = V/C)
$= \frac{2V/c}{2(V^2/c^2)}$
2(1/2)
$= 1 \pm \sqrt{1 - V/C}$
V/c
$=\frac{C}{V}\left[1\pm\sqrt{1-V_{c2}^{2}}\right]$
The state of the s
$= 9/\sqrt{+9/\sqrt{1-V^2/c^2}}$
$= \frac{C_{1}}{2} + \frac{C_{1}^{2}}{2} \left(1 - \frac{V_{1}^{2}}{2}\right)$
- 1/V - 1C)
$= \frac{c}{1} + \frac{1}{1} + $
SCACE TE
But cos0 < 1. 2 believe
7 +1
$\Rightarrow cos0 = \mathbf{E} - \begin{vmatrix} c^2 - 1 \end{vmatrix}$
(: discard (/v + / C/12-1 >1.)
$\Rightarrow \cos 0 = \frac{C}{V} - \left(\frac{C^2}{V^2} - 1\right)^{1/2}.$
$=\frac{C}{V}-\frac{C}{V}\left(1-\frac{V_{/2}^{2}}{V}\right)^{2}$
$=\frac{C}{V(1-(1-V/c^2)^2)}$
76/
= ///- 21 / / / / 2
$= \frac{1}{\sqrt{1-\frac{1}{2}}} \left(-\frac{1}{2}\right) + \frac{1}{2}\left(\frac{1}{2}-1\right)\left(-\frac{1}{2}\right)^{\frac{1}{2}}$
2
Scanned with CamScar



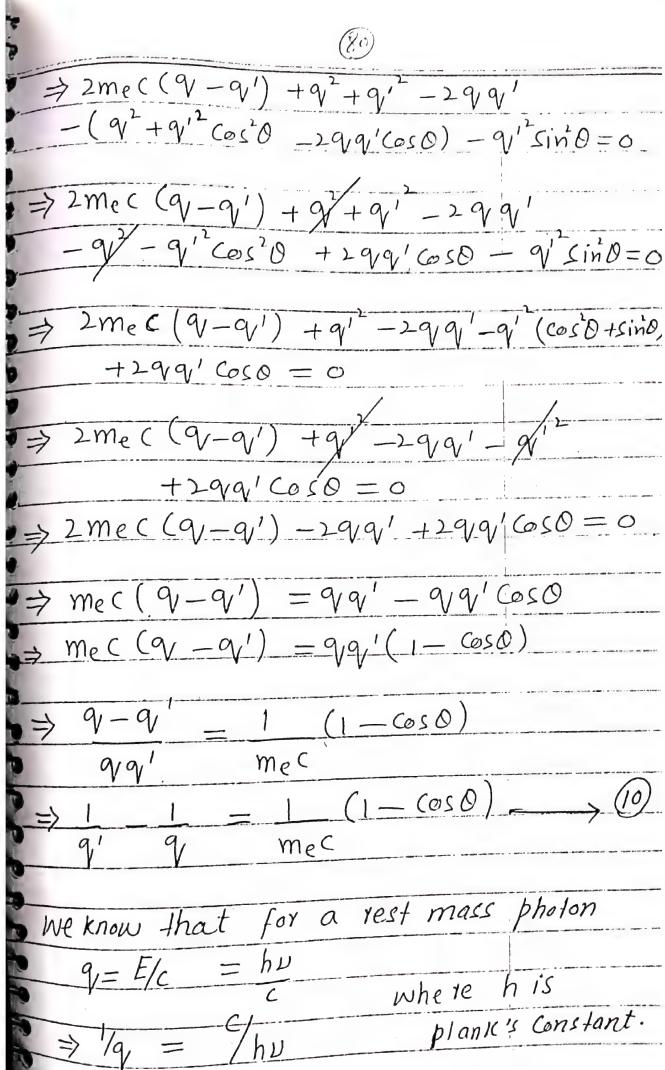


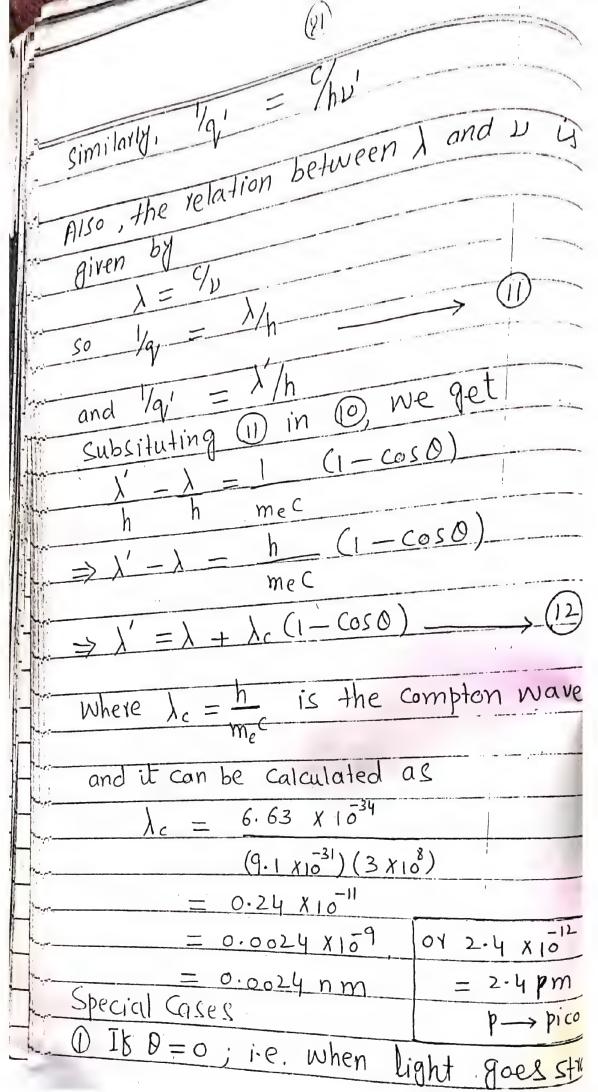
(empton Eppect: According to the quantum theory of light, photons behave like particles except for their lack of rest mass. We shall examine the collision of photons with electrons. Consider light (photons) incident on electrons at rest. The scattering of a photon by an election is called compton effect. Energy and momentum are conserved in such an event and as a result the scattered photon has less energy than the incident photon. We want to study this effect in iclativistic telm. For this purpose, we consider a collision between a single photon and an electron. Let us assume that p'and q' represent the momentum 4-vectors of an electron and that of photon before collision and furtherm p' and q' represent the momentum 4-vector of electron and photon after collision. Let us assume that after the collision, the photon goes off at an angle o relative to the direction of motion while the election goes off at an angle 9, measured in opposite sense to O. Scanned with CamScanner

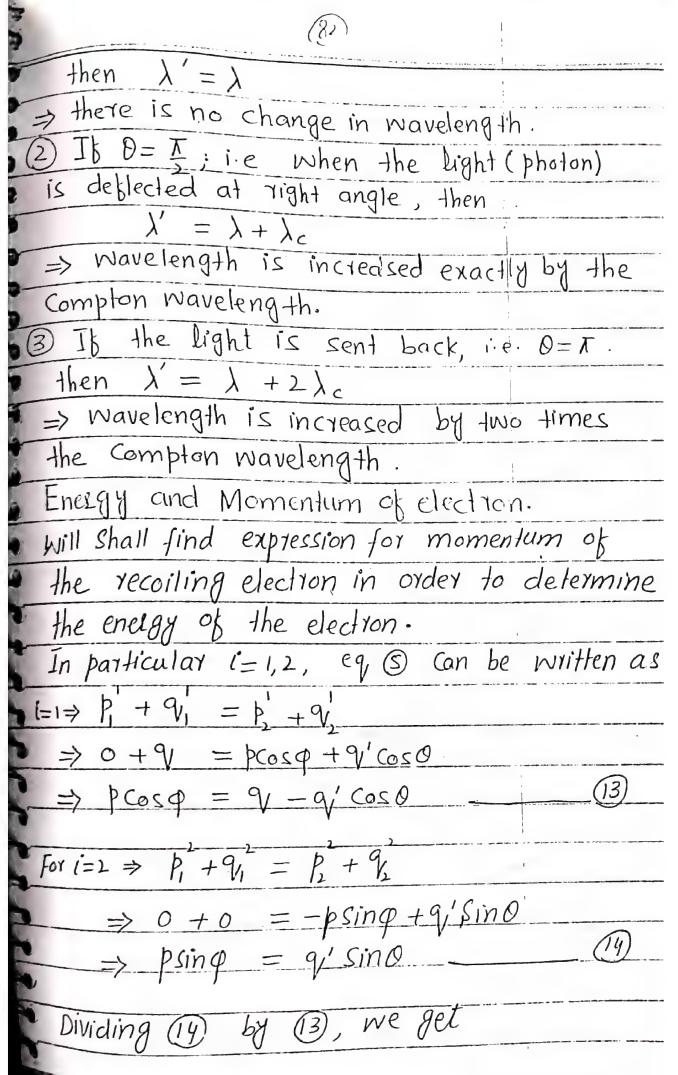


After the collision, the momentum of electron is and the momentum of photon is $q'_1 = (q'_1, q'_1 a'_1)^{3}$ (coso, q'sino, 0) By the law of conselvation of momentum Thus, in Minkowski Space, we have gi pi pi = gi, (pi + qi - qi) (pi + qi - qi) = 9ijp'p' + 9ijp'(9, -92) + 9ij p'(q,'-q,') + 9ij (q,'-q,') (q,-q) $= \frac{g_{ij} p_i^{i} p_j^{j} + g_{ij} p_i^{i} (q_i^{j} - q_j^{j})}{+ g_{ij} p_i^{i} (q_i^{j} - q_j^{j}) + g_{ij} (q_i^{i} - q_j^{i}) (q_i^{j} - q_j^{j})}$ July dummy gijpi'pi + 2 gijpi(qi - qi) +9i; (qi-qi) (qi-qi) in room that the squared magnitude

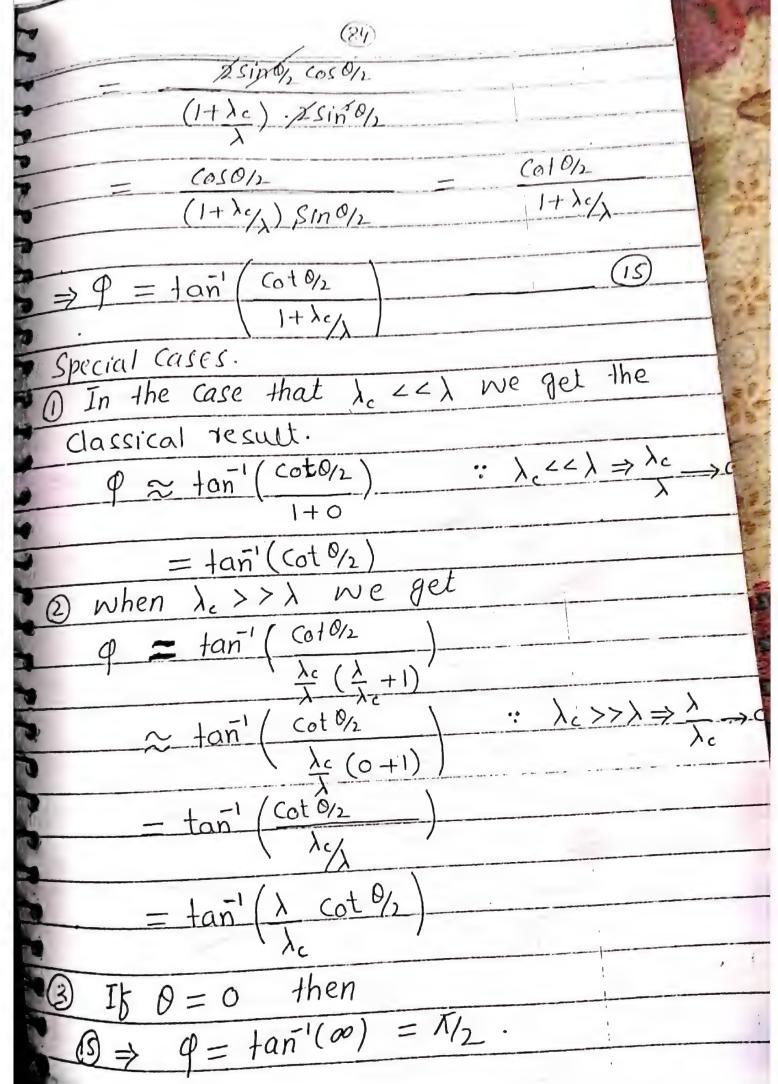
of momentum 4 vector is The free man thus, Sij P. P. - me C 8) mg (+ 19/2, (9, 1 - 9, 1) + 81; (9, -9,1) (9, -9,1) => 28ijpi(q, '- q, ') + 8ij (q, '-q')(q, '-q') => 2 800 P° (Vi - Vi) + 28+1 Pi (9i - 9i) +29, P.(9, -9,) + 2-933 P.(9, -9,)+ 800 (90° - 90°) (90° - 90°) +911 (91' - 912) (91' - 9 +9,2(9,-9,2)(9,-9,2)+9,2(9,3-9,3)(9,5-1)Putting 900 = 1; 911 = 922 = 933 = -1, We 9 2p (91 - 91) - 2p (91 - 91) - 2p (91 $p_1^3 (q_1^3 - q_2^3) + (q_1^0 - q_2^0) - (q_1^0 - q_2^0)$ $(q_1^2 - q_2^2)^2 - (q_3^3 - q_2^3)^2 = 0$ Substituting egs D, @ and (y) in eq, (9), we get 2me((9-9') -0-0-0+(9-9') $-(9-9'\cos 0)^2 - (0-9'\sin 0)^2$ => 2mc ((q,-q') + (q,-q') - (q-q'(coso)-(

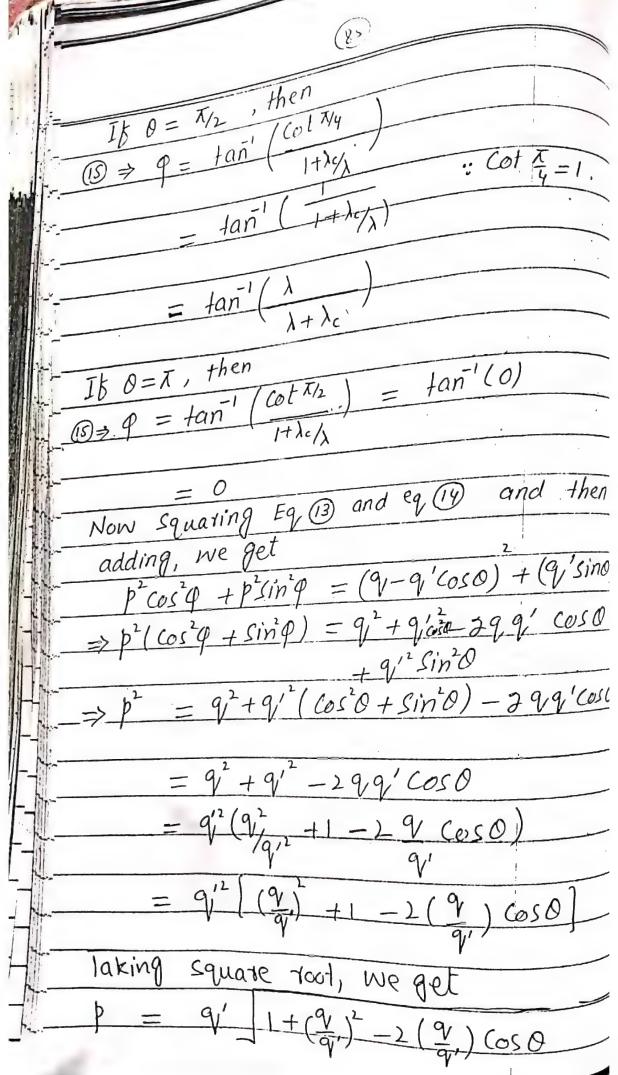


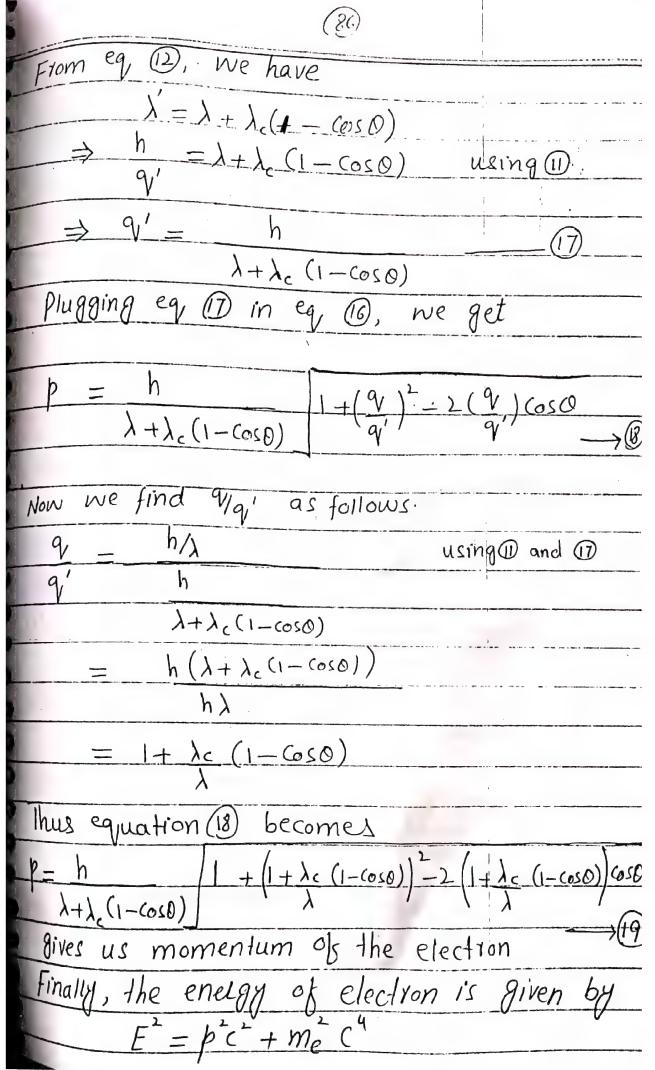




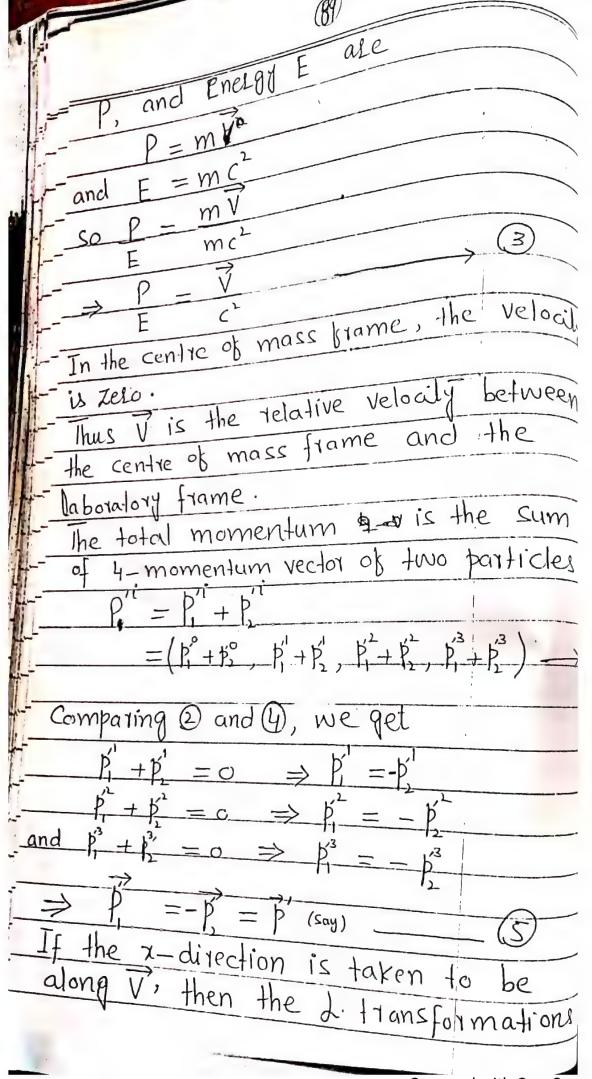
(9.3)	
nein a gisino	
9, -9, 6030	and the second second second .
CINC	
$\Rightarrow \tan \varphi = \frac{q}{q(1-q'\cos\theta)}$	
Cino	
$= \frac{\sqrt{q}}{1} - \frac{1}{q} \cos \theta$	
William Y	
= Maino :us	ing W
$\frac{\lambda}{h} - \frac{\lambda}{h} \cos \theta$	
$\Rightarrow \tan \varphi = \lambda \sin \varphi$	
$\lambda - \lambda \cos \theta$	
- Asino	using (12
$\lambda + \lambda_c (1 - \cos \theta) - \lambda \cos \theta$	
$\frac{\lambda + \lambda_{c} (1 - \cos 0) - \lambda \cos 0}{\lambda \sin 0}$	
$\lambda + \lambda_c (1 - \cos \theta) - \lambda \cos \theta$	
$\frac{\lambda + \lambda_{c} (1 - \cos 0) - \lambda \cos 0}{\lambda \sin 0}$	
$\frac{\lambda + \lambda_{c} (1 - \cos \theta) - \lambda \cos \theta}{\lambda \sin \theta}$ $= \frac{\lambda \sin \theta}{\lambda (1 - \cos \theta) + \lambda_{c} (1 - \cos \theta)}$ $= \frac{\lambda \sin \theta}{\lambda \sin \theta}$	
$\frac{\lambda + \lambda_{c} (1 - \cos 0) - \lambda \cos 0}{\lambda \sin 0}$ $= \frac{\lambda \sin 0}{\lambda (1 - \cos 0) + \lambda_{c} (1 - \cos 0)}$	
$ \lambda + \lambda_{c} (1 - \cos 0) - \lambda \cos 0 $ $ = \lambda \sin 0 $ $ \lambda \sin 0 $ $ (\lambda + \lambda_{c}) (1 - \cos 0) $ $ = \chi \sin 0 $	
$ \lambda + \lambda_{c} (1 - \cos 0) - \lambda \cos 0 $ $ = \lambda \sin 0 $ $ \lambda \sin 0 $ $ (\lambda + \lambda_{c}) (1 - \cos 0) $ $ = \chi \sin 0 $	
$\lambda + \lambda_{c} (1 - \cos 0) - \lambda \cos 0$ $= \lambda \sin 0$ $= \lambda \sin 0$ $= (\lambda + \lambda_{c}) (1 - \cos 0)$ $= \lambda \sin 0$	
$\lambda + \lambda_{c} (1 - \cos \theta) - \lambda \cos \theta$ $= \lambda \sin \theta$ $= \lambda \sin \theta$ $(\lambda + \lambda_{c}) (1 - \cos \theta)$ $= \lambda \sin \theta$	
$\lambda + \lambda_{c} (1 - \cos 0) - \lambda \cos 0$ $= \lambda \sin 0$ $= \lambda \sin 0$ $= (\lambda + \lambda_{c}) (1 - \cos 0)$ $= \lambda \sin 0$	





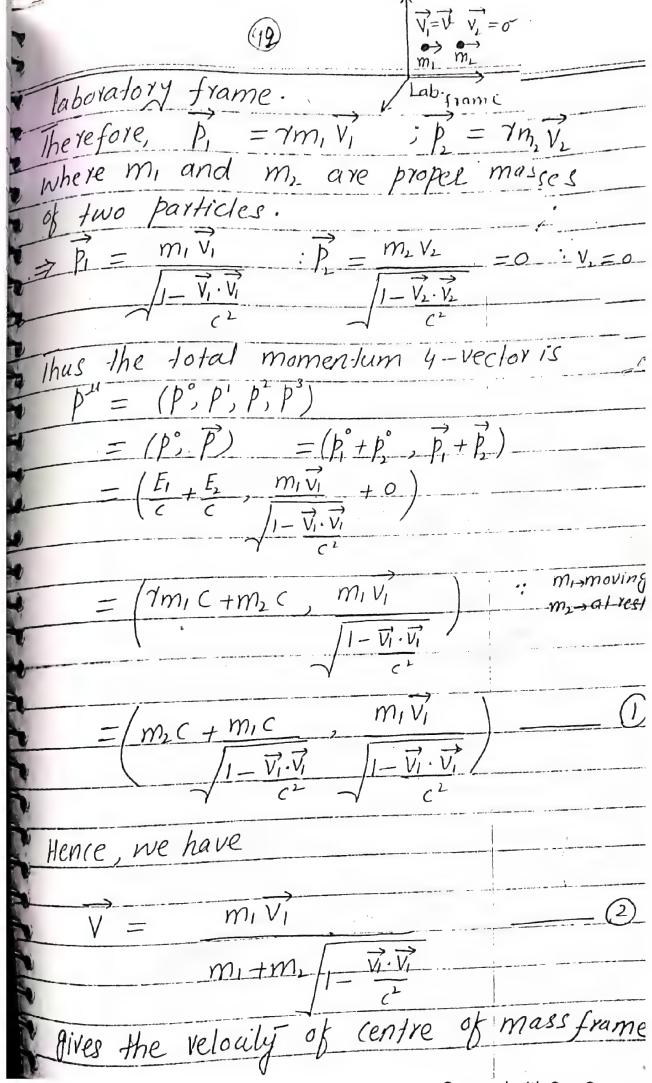


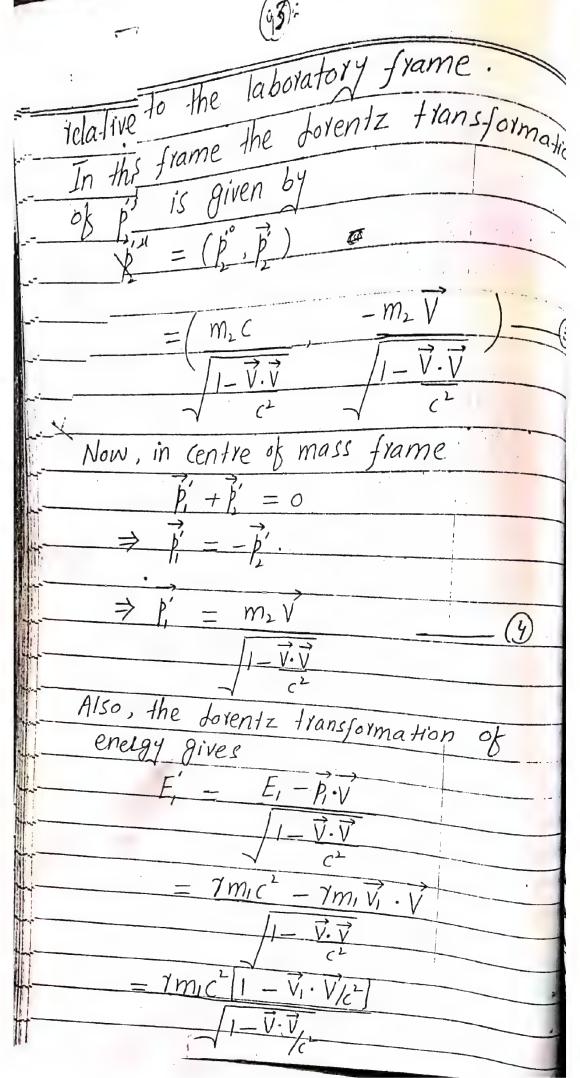
(P)
pc (1 + me c)
P P P P P P P P P P P P P P P P P P P
b2-2 (1 + h2 mc ()
= PC 11 / h' p'
$= b^2 c^2 \left(1 + \frac{h^2}{b^2} \cdot \frac{\text{me } c/h}{}\right)$
$= b^2c^2\left(1+\left(\frac{h}{h}\right)^2 m_e^2 c^2/h^2\right)$
$= p^2c^2\left(1+\frac{h}{p}\right) m_e \left(\frac{h}{h}\right)$
= pc2 (1+ le me c/h2)
= PC (1+ Ne THE C / M)
The De Rycolie Mount
where he is the De Broglie Wavele
of the electron.
$\Rightarrow E = \frac{ c }{1 + \lambda_e^2 m_e^2 c^2/2}$
$= \frac{PC}{1 + \lambda e/2}$
- / \c
where $\lambda_c = h$ is Compton way
Me C
Eq 20 including 19 gives us the ene
of electron.
(Ex) what is difference 1
and centre of marie a between labora lorge
and centre of mass frame. Also find the
Components in the laboral in the
Components in the laboratory Stame
the two particles. Tames
Scanned with CamScanner

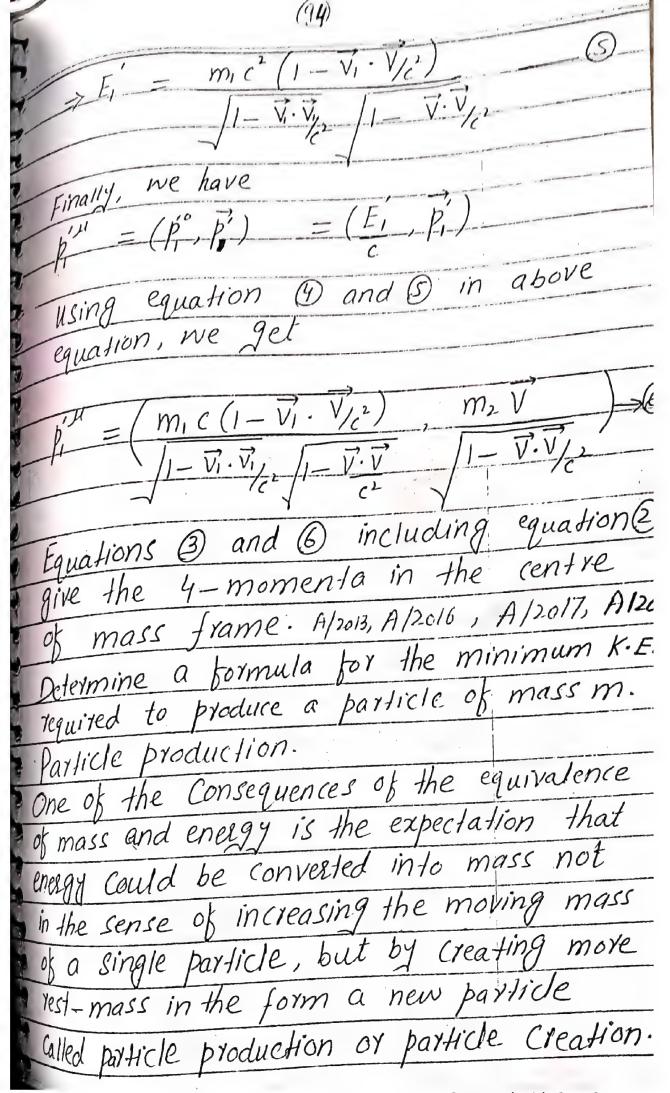


relating the laboratory frame to the
trame are given by
P12 = 7 (P/2 - V P'°)
$= \gamma \left(p_{1x} - \frac{\nabla}{c} \cdot E_{1/c} \right)$
F V/2
1- V/c2 " using (5)
h h' l'
$P_{1}y = P_{1}y = P_{2}'$ $P_{2} = P_{2}' = P_{2}'$ using (5) $P_{1}' = P_{1}'$
and
$P_{x} = 7(P_{x} - \frac{VP'^{\circ}}{2})$
$=7(P_{12}-\frac{V}{C},\frac{E_1}{C})$
C. C.
$=-\frac{P_{2x}-E_{2}}{V_{c}^{2}}$ using (5)
$\frac{1-\sqrt{2}}{2}$
101 P = - P2 - E2 Vc2
$\frac{101}{1-\frac{1}{2}} = \frac{1}{1-\frac{1}{2}}$
$\frac{P_{2y}}{P_{2y}} = \frac{P_{2y}}{P_{2y}} = P_$
The energy momentum of 1st particle is
$E_1 = \gamma (E_1' + P_2' \vee)$
A count of provided advantage and business.

$\Rightarrow E_1 = E_1 + P_2 V$ $L = V_{C1}$
$\Rightarrow E_1 = \frac{1}{1 - \frac{1}{2}}$
L=V/c
and of second particle is
- and of second part
F. = Y(E' P'_X V)
\bot = E_1 - P_2 \vee
1-1/2
Li- Franchia 2.17
Example; 2017 Describe particle contraction
Describe particle scattering by Consider
two particles having face vector momenta
" The 1900 19-1014 frame hu
11/1/27 4/0/0-
Let us consider a particle of yest mass
m, and velocity V' = 12 b Yest mass
a particle of mace vo
in laboratory frame. at rest i.e. V = 0
- Training
In laboratory frame. We can write the and 3-momenta pulling the
and 3-momentum vectors P and Fu
Since the low particles are
particles are in halling
Scanned with CamScanner

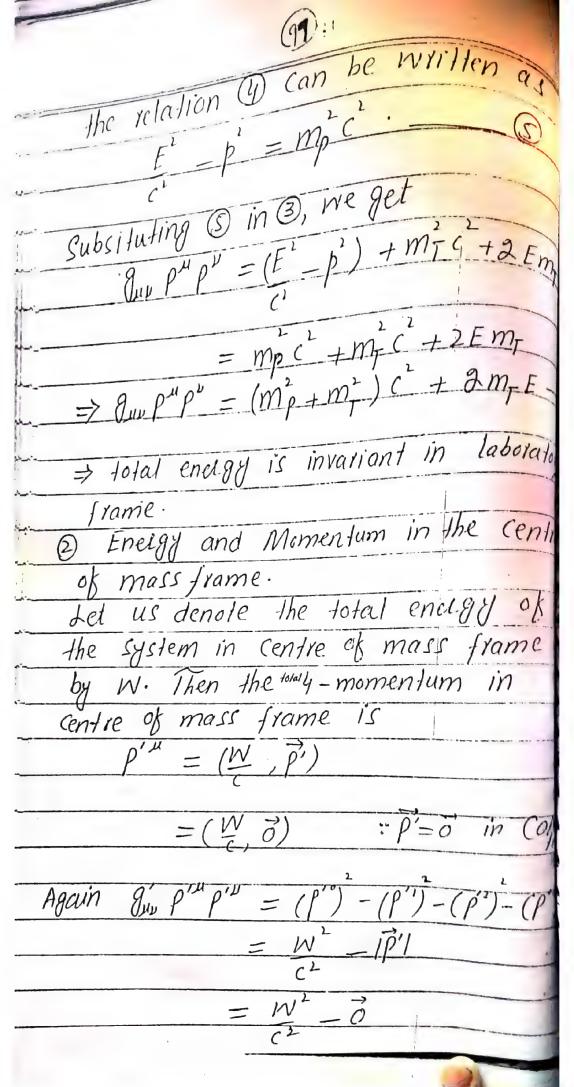






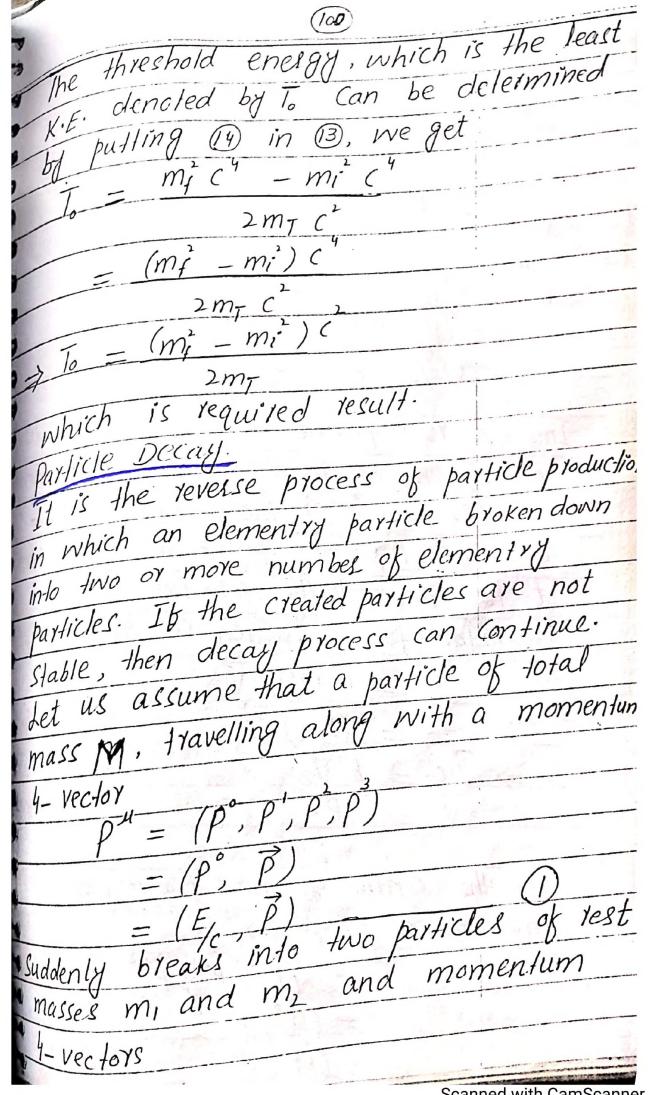
(45)
For this purpose, let us correider a partice
This hulpose, let us I - 1018
For Mis partain velocity, ve call
moving with wind Life:
this particle as projective particle. This This particle strikes another particle this particle strikes and the target particle
This particle strikes anomore in this
This particle strikes This particle strikes particle moves off and the target particle
particle moves 11
moves as well. We further assume that the Collision of
We further assume mater a new partie
these two particles generates a new particle
Let us denote the rest-mass of the three
particles by mp (for the projectile), my (for
the target particle) and mn (for the new
particle produced).
For given masses of these particles, we
want to calculate the minimum K. E.
required to produce a new particle.
For this puspose, we find the energy
aria momentum of these particles in
The Laboratory frame and in the centre
of mass trame.
O Energy and Momentum in laboratory
The state of the s
Let E be the energy of the projectile
of mass mp in the laboratory frame.
Then the 4-vector momenta of the
projectile and the target particles
Scanned with CamScann

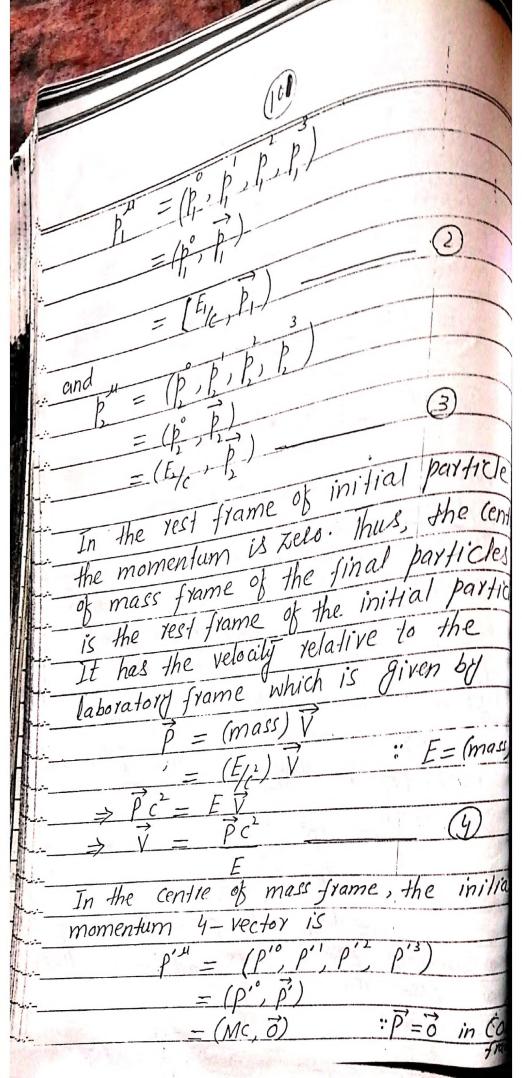
would be $=(E_{/c},\vec{P});\vec{P}_{r}=(m_{,c},o)$ where Pp and pu denote the 4 vector momenta for projectile and target particle respectively. Thus, the total 4-vector momentum before Collision is (P, P, P, P) Pp + p= = (E/e+m-c, P) (2 Squared magnitude in Minkowski space (E/c+m_c) - 1/12 = E/c + mfc + 2 Emfc - p2 S mass relation is given by The $-p = m^{-1}c$ the total momentum-energy before the Collision. particular, for the projectile of mass

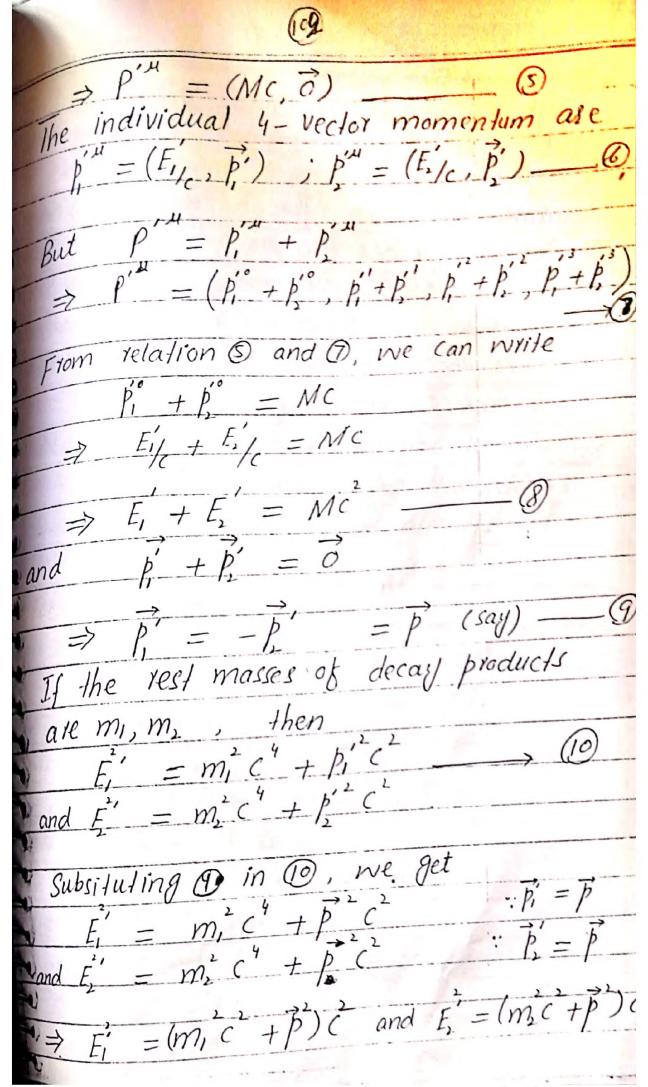


(A) 8)
3 A' P'MP'U
Jun P'P' = W/c2 = 7
10/4 managinal
of 9-100 that the country
magrirual of 4-momentum vector in
Inbotatory frame should be equal to
4-momentum vector in Centre of mass
a DIN DIN
The space
Spail
Subsituting 6 and 7 in above relation,
Subsituting 6 and 9 in above relation, we get
$\frac{W^{2}}{c^{2}} = (m_{p}^{2} + m_{f}^{2})c^{2} + 2m_{f}E$
$\Rightarrow \frac{W^{2} - (mp^{2} + m_{T}^{2})c^{2}}{c^{2}} = 2m_{T}E$
$\Rightarrow E = W/c^2 - (mp + m_T)c - 8$
$2m_T$
which is total energy of the projectile
in laboratory frame.
To find the mass mn, for new particle,
we can write the final mass as
$m_f = m_p + m_T + m_N = 9$
where my denotes final mass.
The K.E. of the projectile, 1, is given by
T. Of The production

(9)
mo ale get co
I = E np c we get lo
1 = 1 mp (2) mp (2)
Subsituting 8 mp + mp (2 mp + mp (2)
$\frac{Subsituting @ in (0)}{I = W/c^{1} - (mp^{2} + mr^{2}) c^{2}} = mp c^{2}$
$\frac{1}{1} = \frac{1}{2m_{1}} \frac{2m_{1}}{m_{1}^{2}} \frac{2m_{1}}{m_{1}^{2}} \frac{2m_{1}}{m_{1}^{2}} \frac{m_{1}^{2}}{m_{1}^{2}} \frac{2m_{1}}{m_{1}^{2}} \frac{m_{1}^{2}}{m_{1}^{2}} \frac{2m_{1}}{m_{1}^{2}} \frac{m_{1}^{2}}{m_{1}^{2}} \frac{2m_{1}}{m_{1}^{2}} \frac{m_{1}^{2}}{m_{1}^{2}} \frac{m_{1}^{2}}{m_{1}^{2}}$
W/c - (mp +111)
2 mT
- m/c - (mp + m7 + 2 mp m7) C
- W/c - (11)
2mT
2 2
$W/c^2 - (mp + m_T) $
$2m_T$
Let us introduce initial mass by m
as $m_i = m_p + m_T$
Then, equation 1 be comes
$\overline{I} = w_k^2 - (m_i)^2 c^{-1}$
$\frac{1}{1} = \frac{VV/C}{VV(i)} = \frac{VV/C}{VV($
$2m_T$
= $W - mic$
$= W - m_i c'$
$\frac{2m_T c^2}{\sqrt{2m_T c^2}}$
in the centre of mass
Can be written as frame $E = mc+1$
" us
$W = m_{f}^{2} (4 + (0)) c$
$\Rightarrow N = m_f c^4$
(14)
Scanned with CamScanner







 $\Rightarrow E_i = \int \vec{p}' + m_i' c'$ and $E_{\lambda} = \vec{p} + m$, $\vec{c} \in C$ Since there are three equations for th Sixo parametess M, P, E, , E, , m, and m; , therefore, we need to know thro of them to determine the other three Once these are worked out, the relevan 4-vectors can be transformed by the Lorentz transformation given by as mentioned in equation (4).